



GRAVITATIONAL INSTABILITY IN IRRADIATED DISCS

*Sahl Rowther, Daniel Price, Christophe Pinte,
Rebecca Nealon, Farzana Meru, and Richard Alexander*

 sahl.rowther@leicester.ac.uk  sahl95.github.io





When are Discs Gravitationally Unstable?

- In their youth, discs can be massive enough that the *disc's self-gravity is important*.
- When the disc mass is comparable to its host star ($\gtrsim 10\% M_{\star}$), gravitational instabilities (GI) can occur resulting in *spiral arms*.



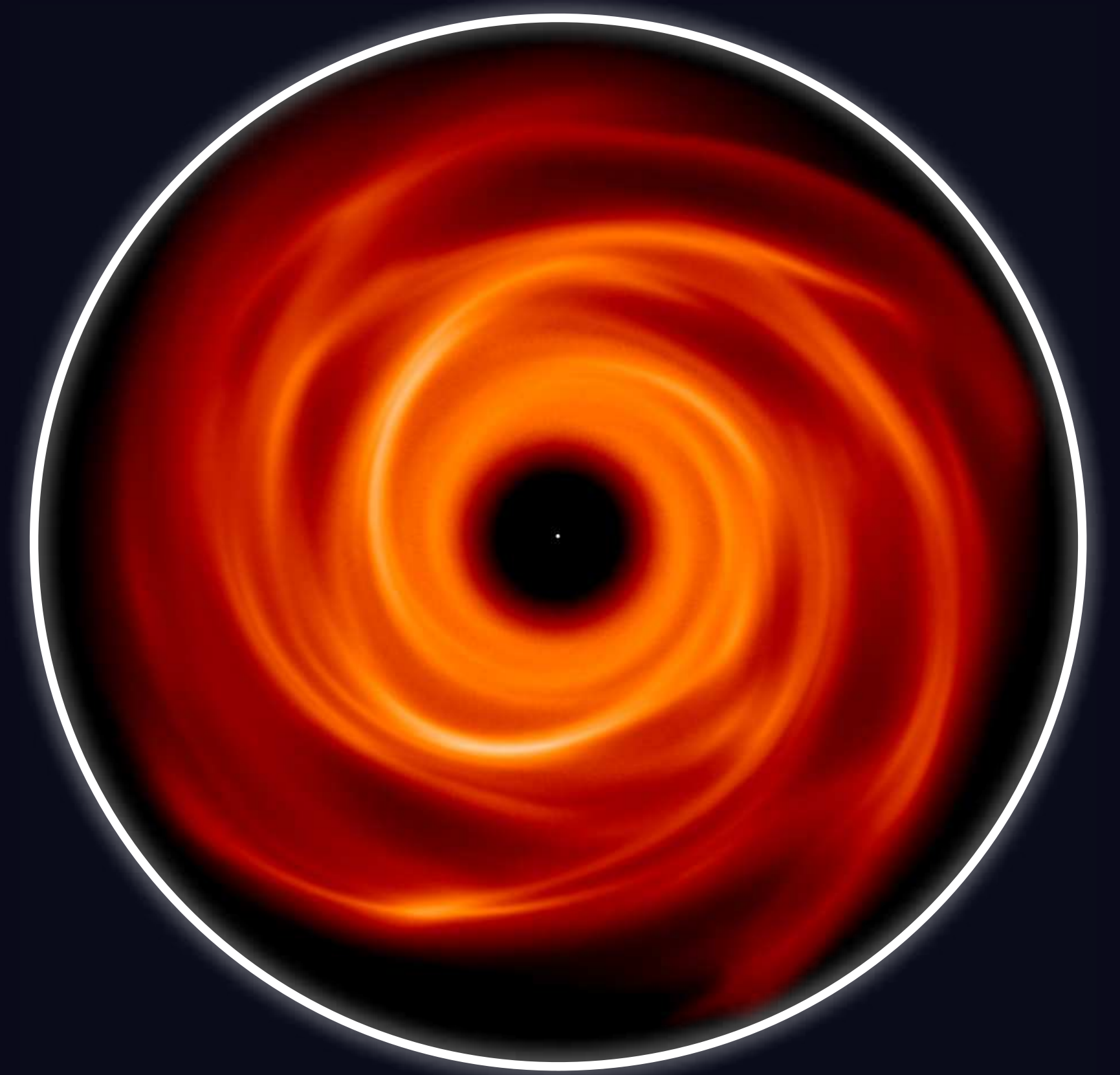
When are Discs Gravitationally Unstable?

Sound speed

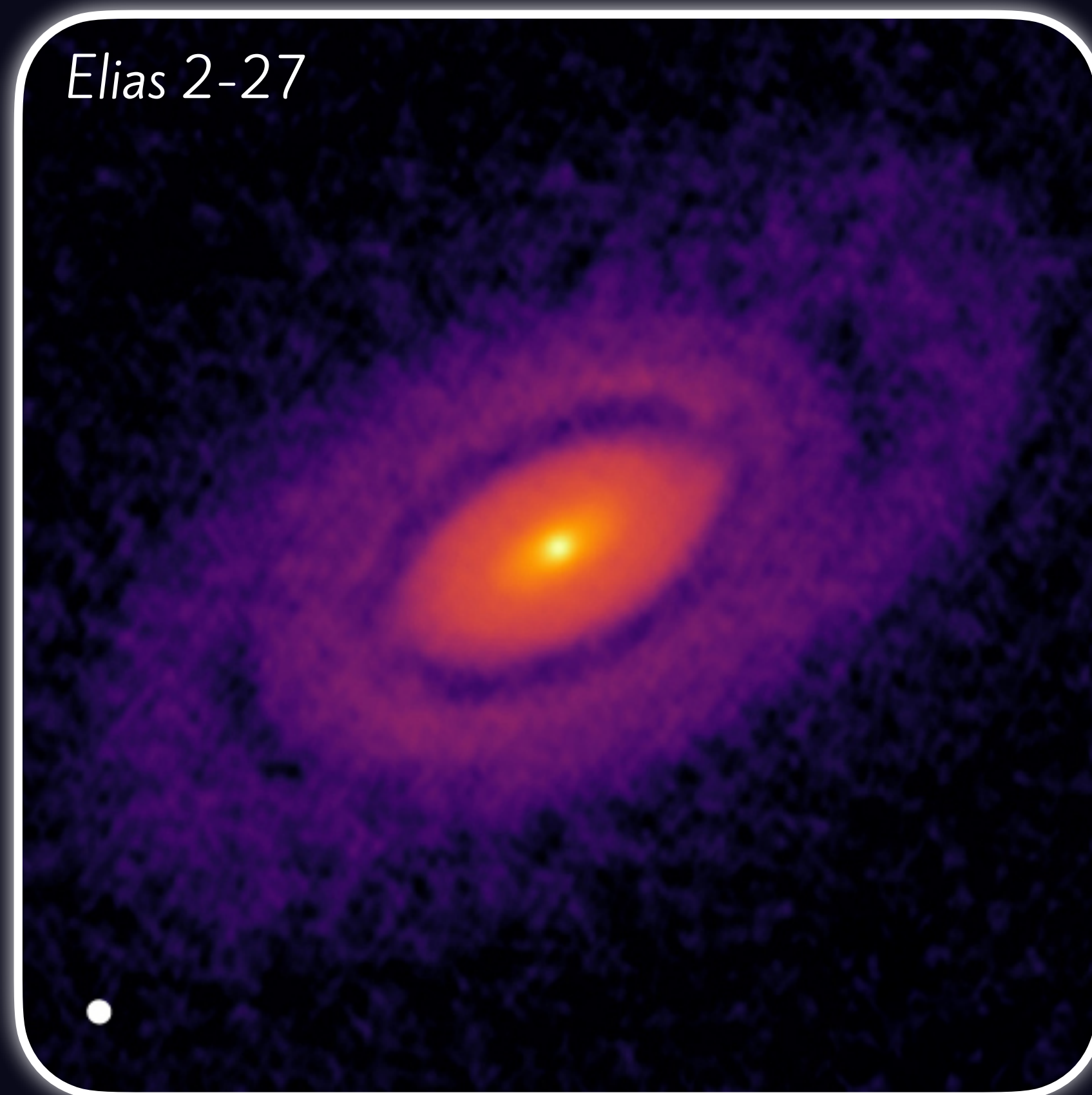
$$Q = \frac{c_s \Omega}{\pi G \Sigma} \gtrsim 1.7$$

Surface Density

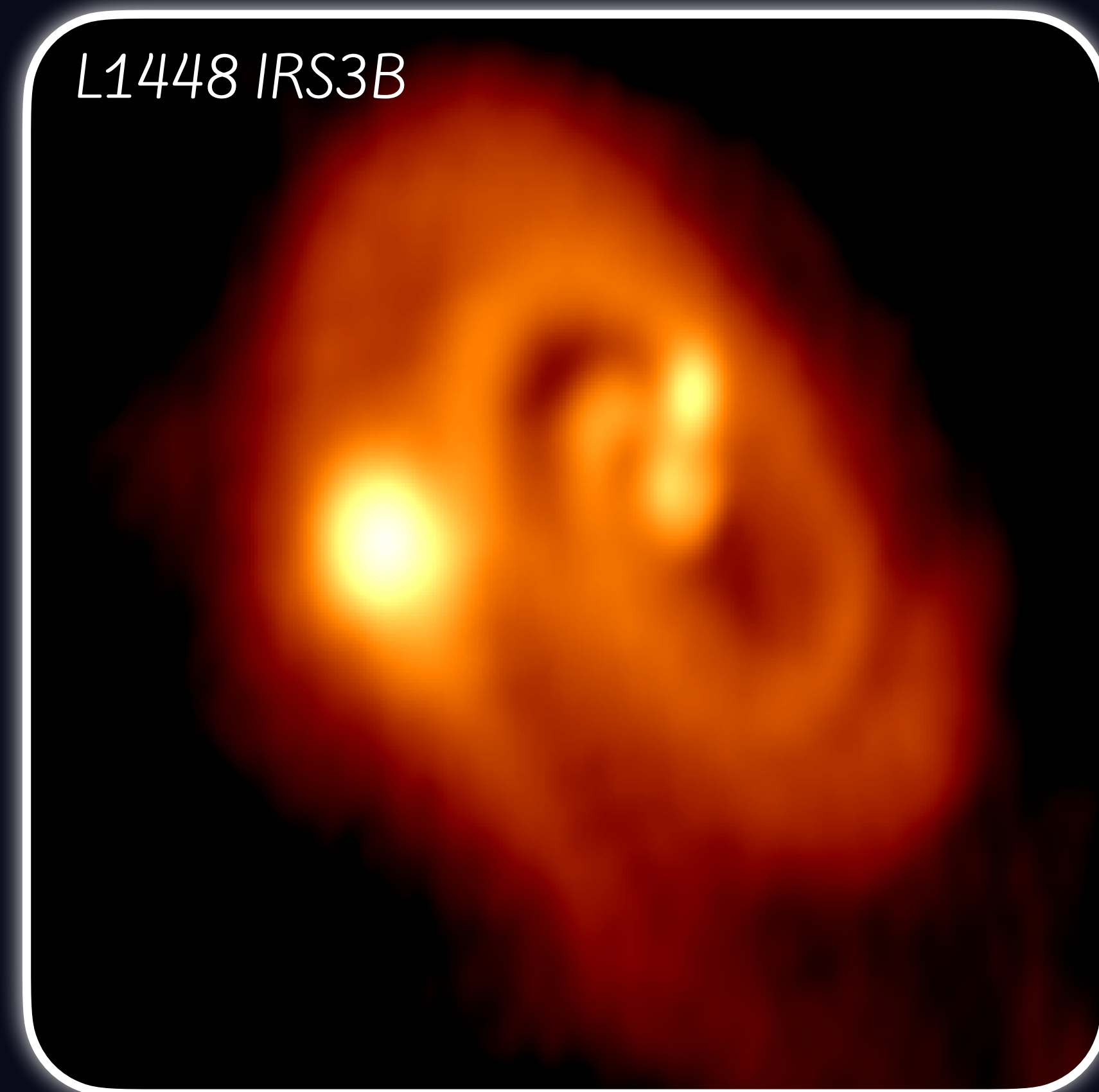
Toomre 1964



Observations of Gravitationally Unstable Discs



Andrews+ 2018, Huang+ 2018



Tobin+ 2016, Reynolds+ 2020

Thermodynamics

Radiative Transfer

- + *Models the disc realistically.*
- *Slow and computationally expensive.*

β cooling

- + *Fast and computationally inexpensive.*
- *Disc model is not consistent with expectations.*

***SIMULATING GRAVITATIONALLY UNSTABLE
DISCS WITH β COOLING***

The Internal Energy Equation

$$\frac{du}{dt} = - \frac{P}{\rho} (\nabla \cdot \mathbf{v}) + \Lambda_{\text{shock}} - \frac{\Lambda_{\text{cool}}}{\rho}$$



*PdV
Heating*



*Shock
Heating*

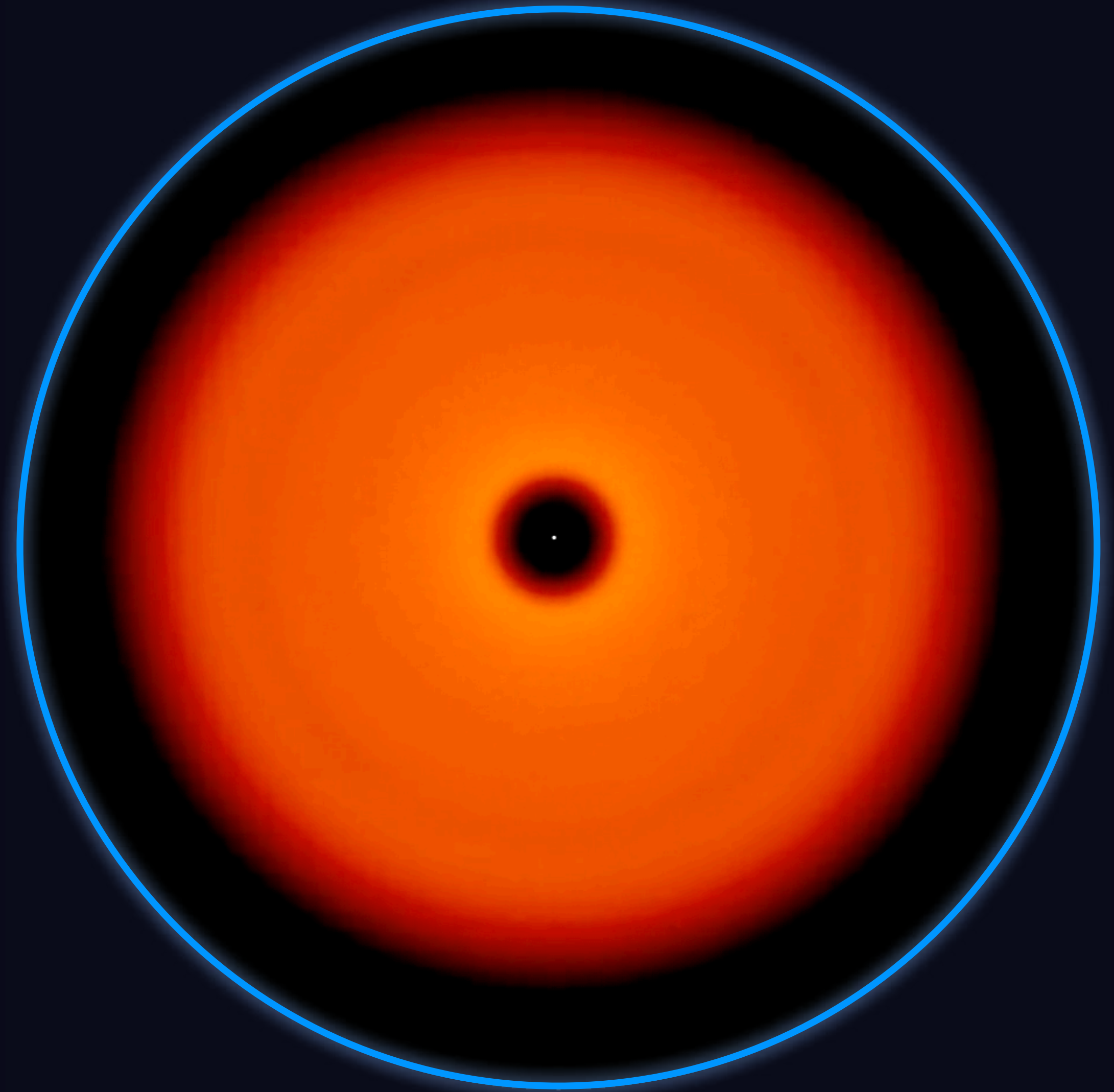


*Cooling
Term*



High Toomre Q

- *Very little PdV or shock heating.*
- *The disc is free to cool until gravitational instabilities develop.*





Low Toomre Q

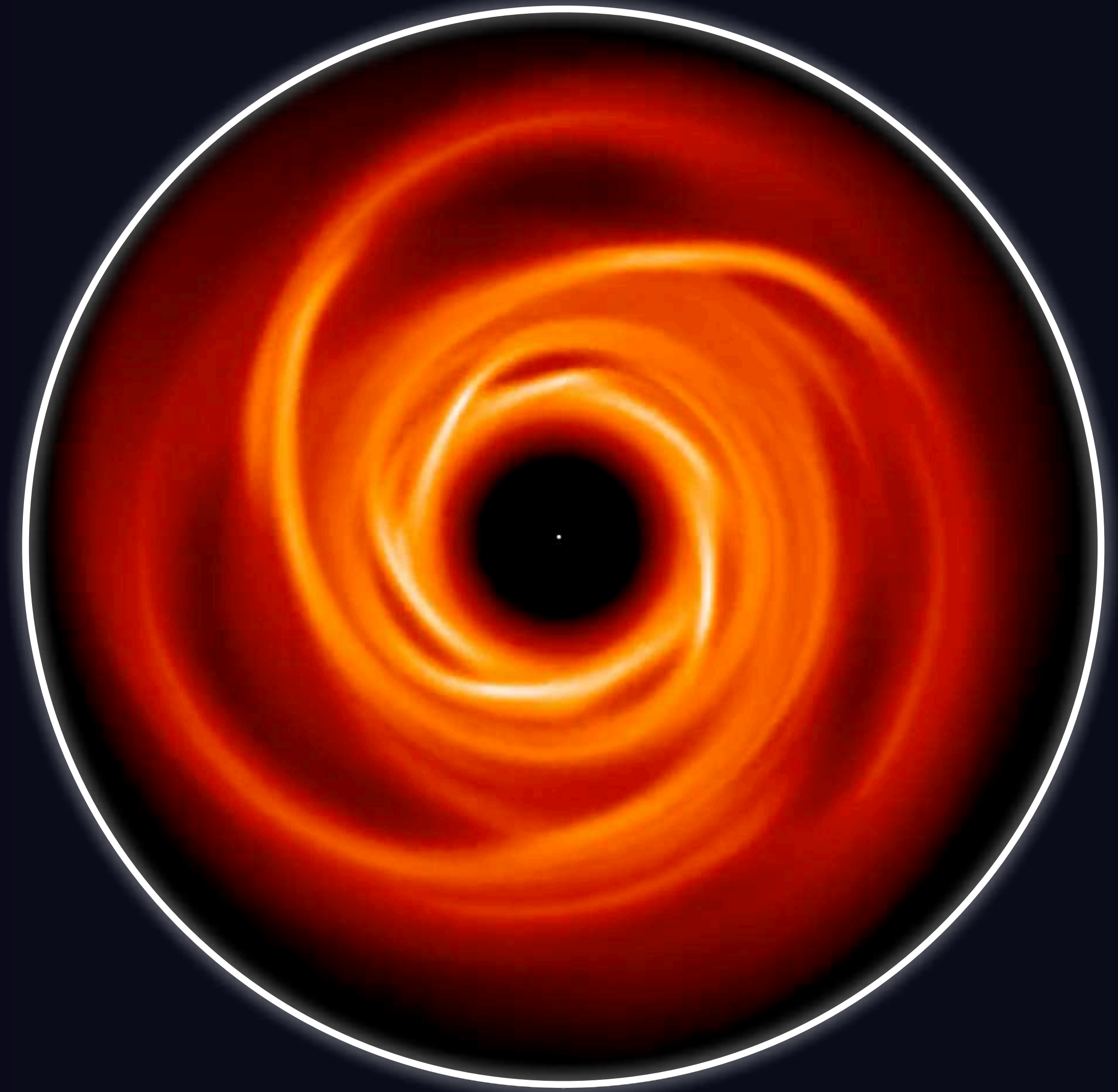
- *Dense spiral structures have formed.*
- *PdV and shock heating become more important.*





Heating and Cooling in Balance

- *PdV and shock heating balance the cooling in the disc.*
- *The disc cannot fragment. Or become stable.*
- *It will remain gravitationally unstable with spiral arms.*



***SIMULATING GRAVITATIONALLY UNSTABLE
DISCS WITH **RADIATIVE TRANSFER*****



CALCULATES THE TEMPERATURES

- Using the luminosity of the star,
- Particle data from PHANTOM,
- PdV and Shock heating from PHANTOM.



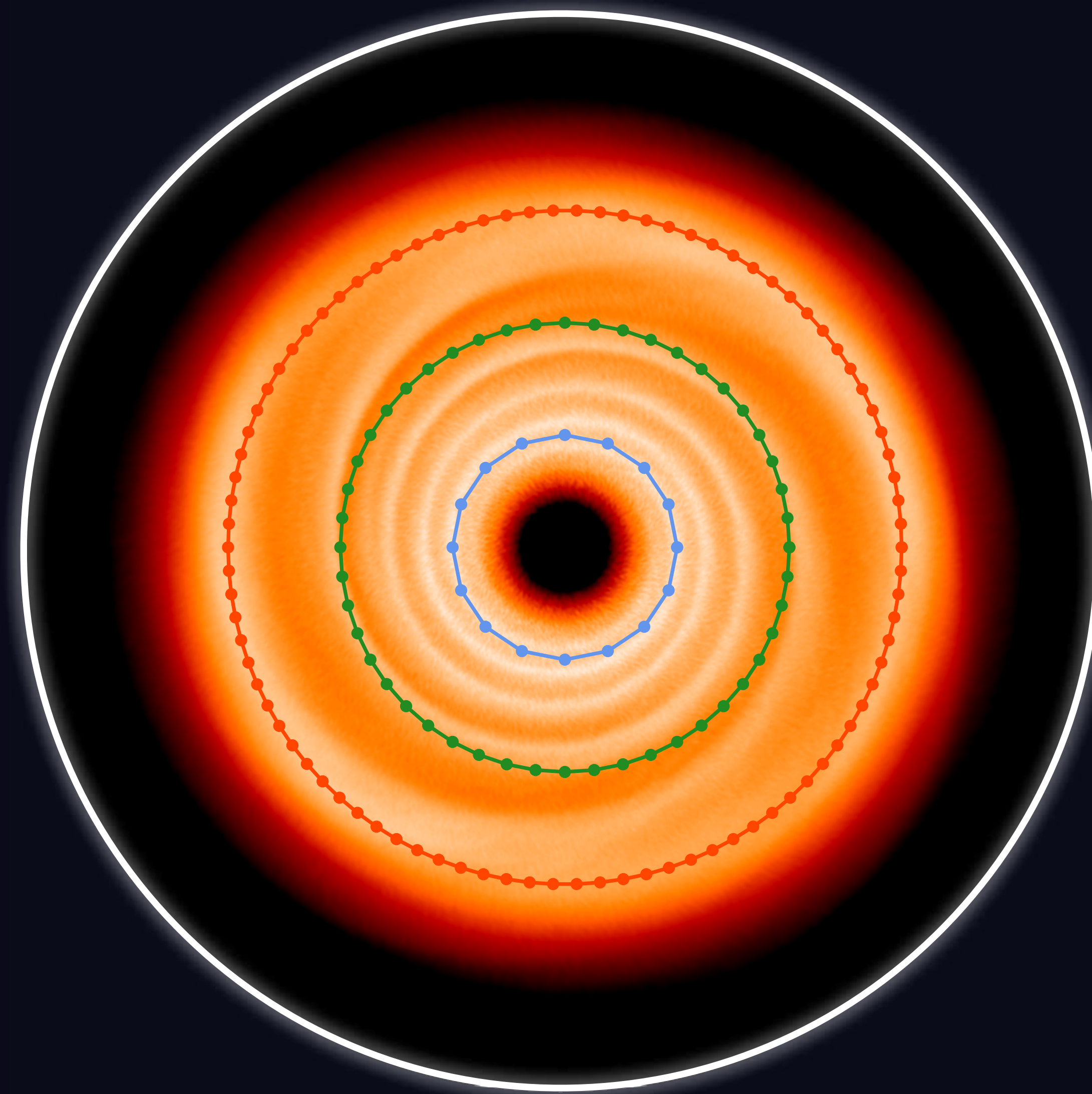
MOVES THE PARTICLES

- Energy is constant between time-steps.
- At the end of each time-step, MCFOST updates the temperatures.



Frequency of calculations

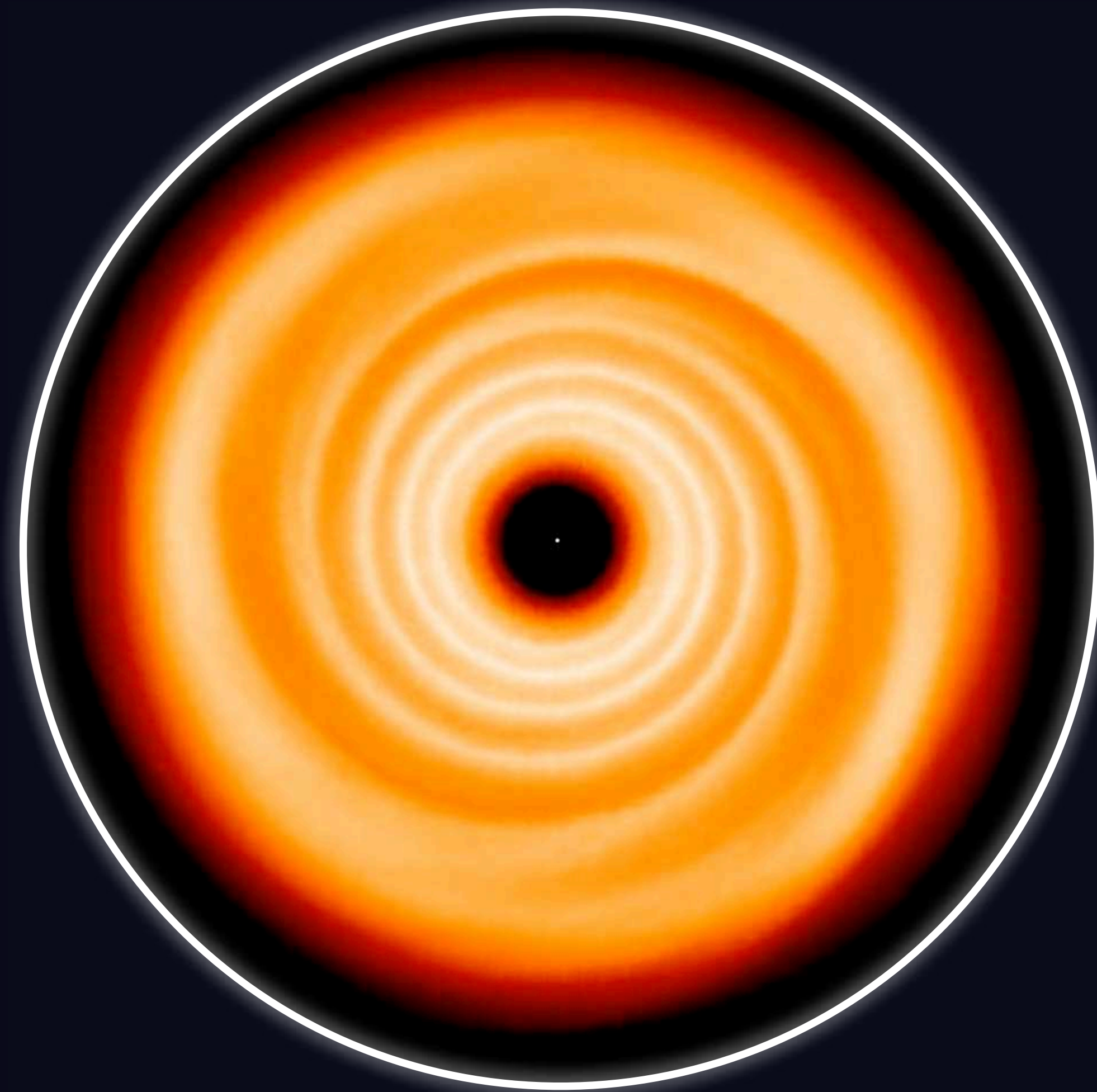
- *The temperature is updated every 7.071 years.*
- *Ensures that particles do not evolve too much between temperature calculations regardless of where they are in the disc.*



How Many Photons?

- *Previous works (Nealon+ 2020, Borchert+ 2022a,b) have used 100 photons for every SPH particle. However, those discs were not as massive.*
- *Gravitationally unstable discs are much more massive, and hence very optically thick.*
- *Need a much higher number of photons to ensure every SPH particle is reached. If no photons reach, the temperature of the particle is set to 2.73K. This results in a negative feedback loop resulting in artificial fragmentation.*
- *We use 5000 photons for every SPH particle.*

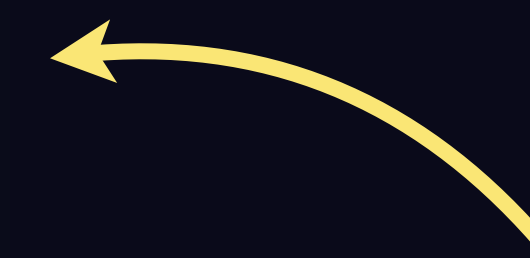
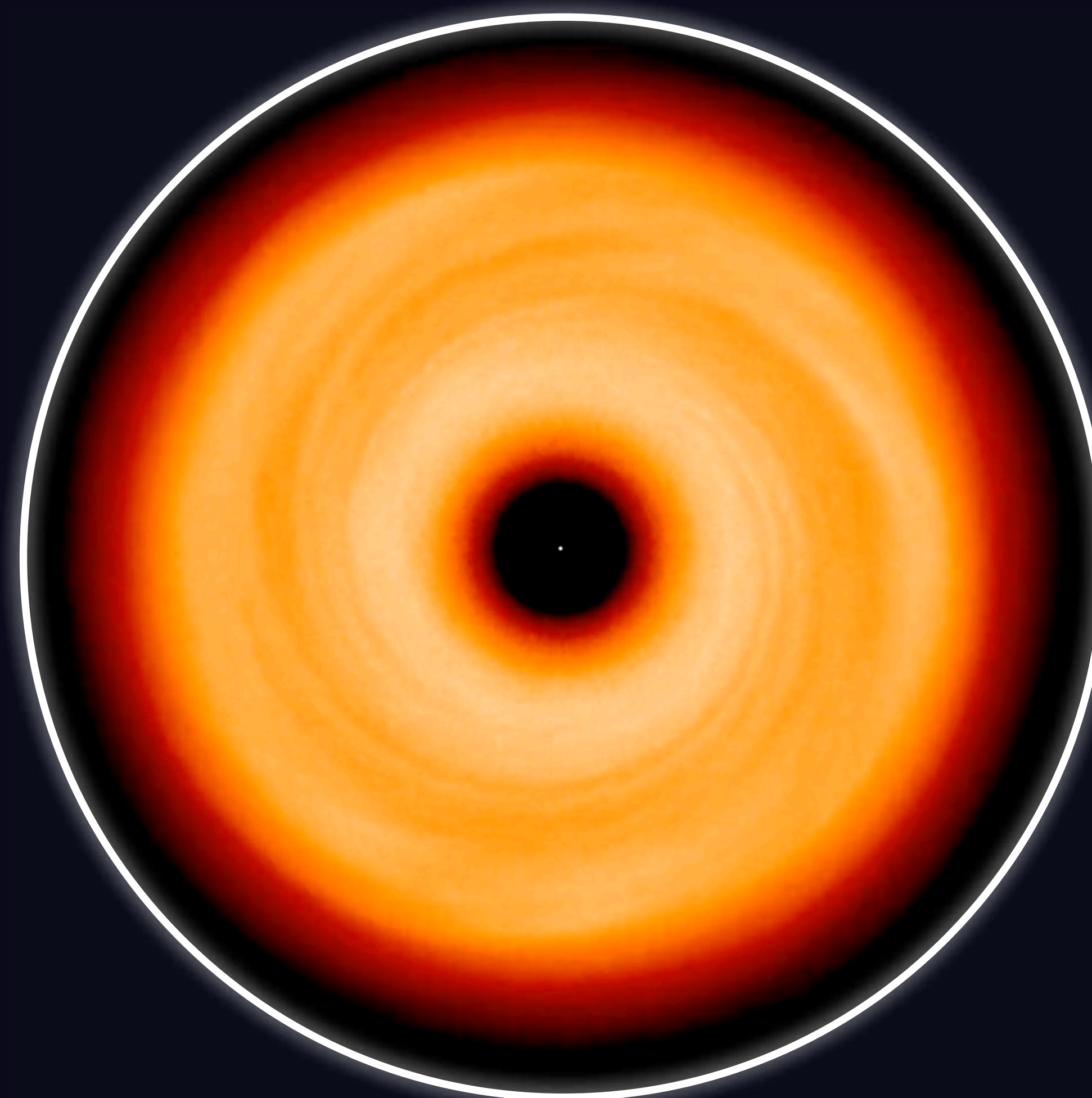
*Evolution of a
 $0.1M_{\odot}$ disc with
Radiative Transfer*



Rowther+ (in prep)



*Evolution of a
 $0.1M_{\odot}$ disc with
Radiative Transfer*



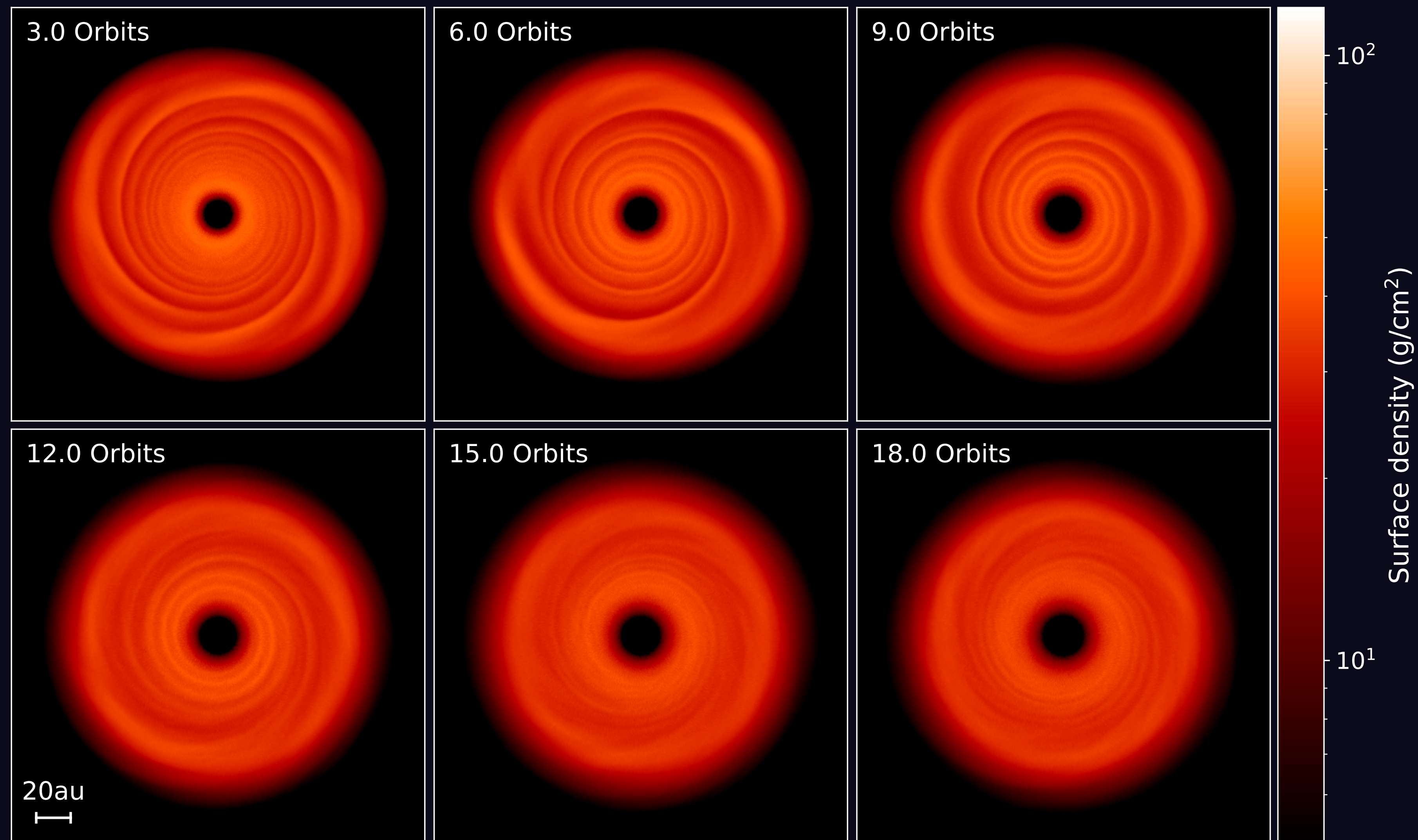
*Gravitational
instabilities
become weaker
over time.*

Rowther+ (in prep)



Radiative Transfer

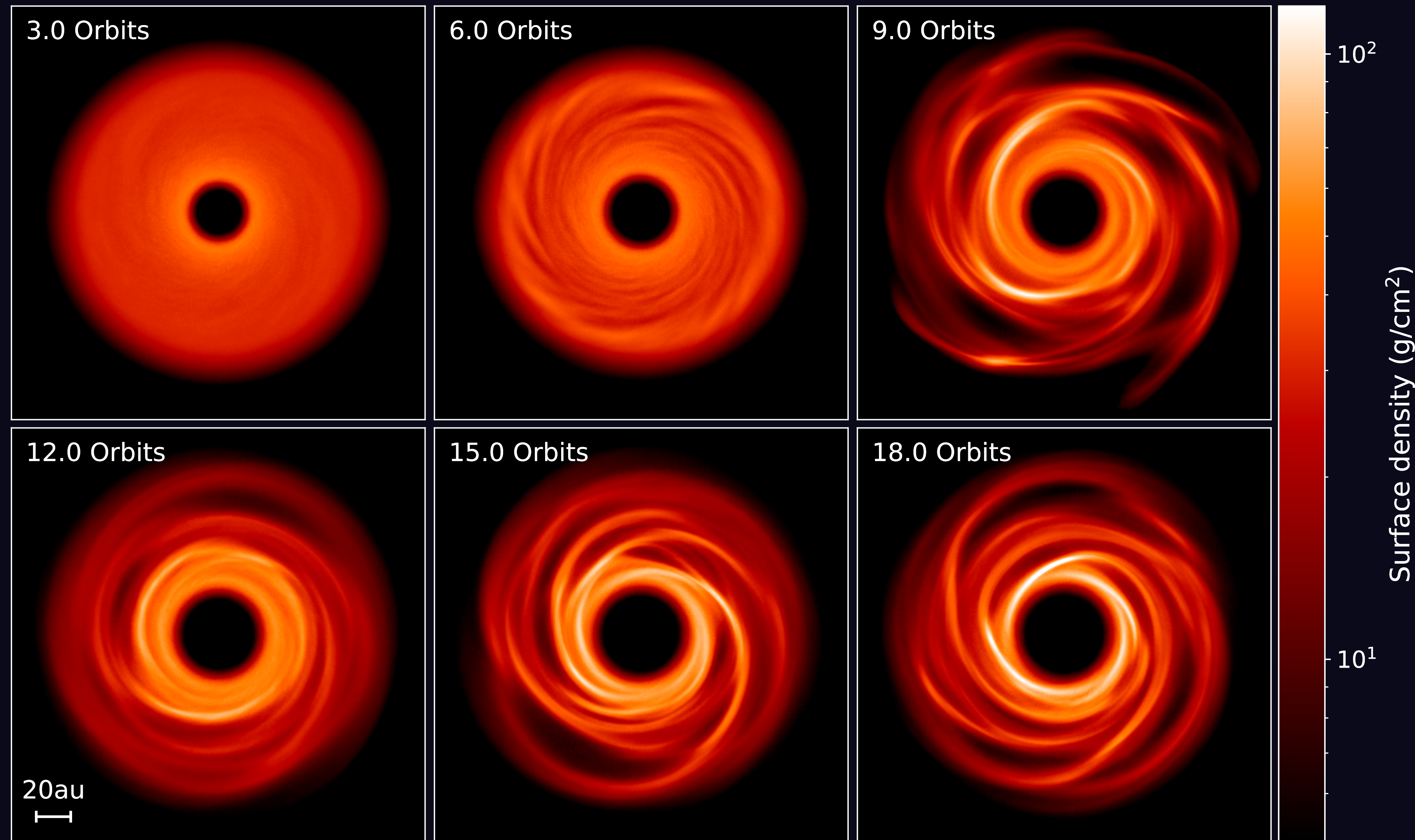
- *Spiral structures are weaker.*
- *Disc becomes more stable over time.*



Rowther+ (in prep)

β cooling

- *Spiral structures are stronger.*
- *Disc is in a steady state with spiral structures.*



Rowther+ (in prep)

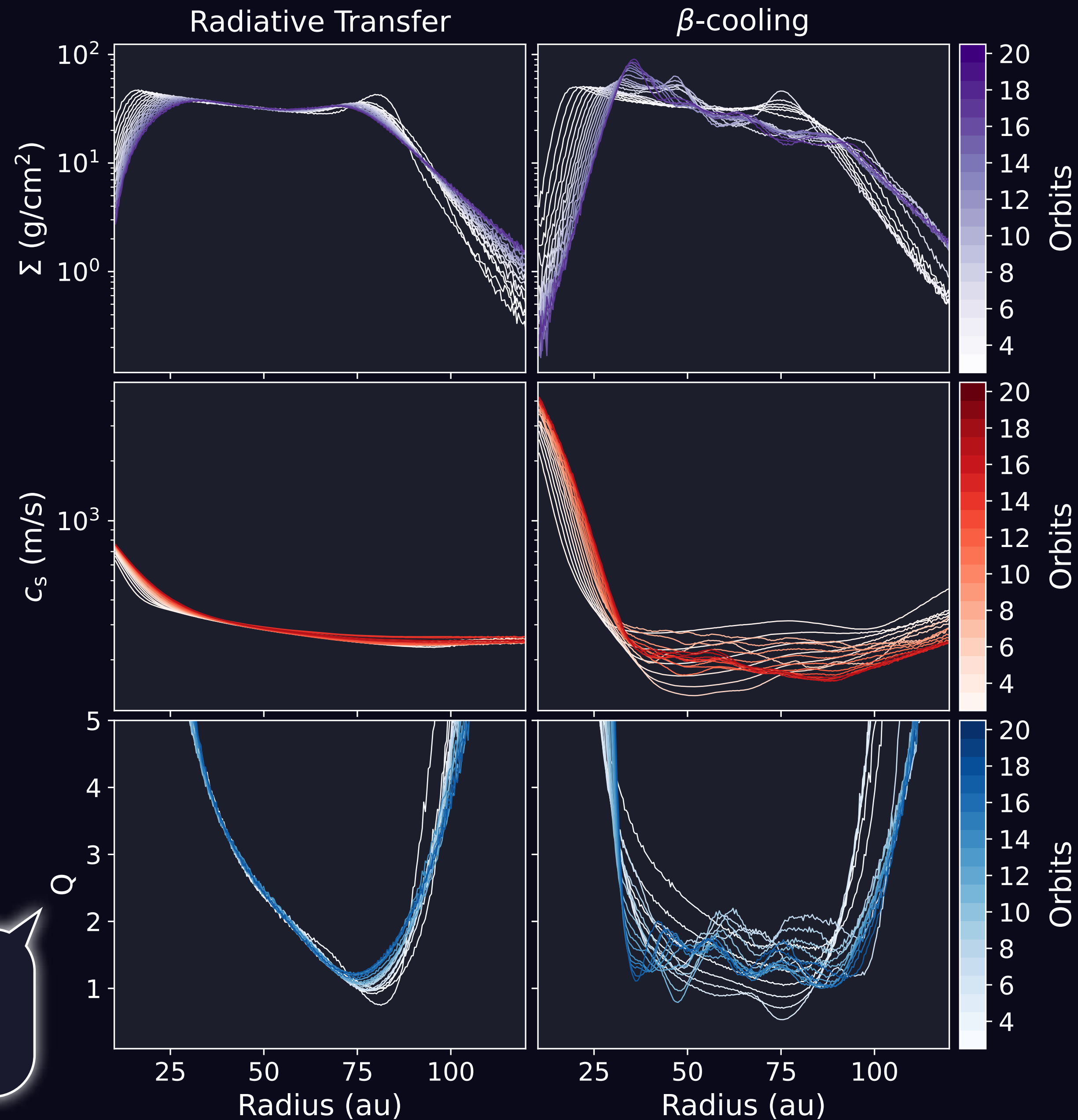


Evolution of Disc Instability

Radiative Transfer

- Disc is warmer.
- Temperature is fairly constant.
- Q has a steady increase.

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



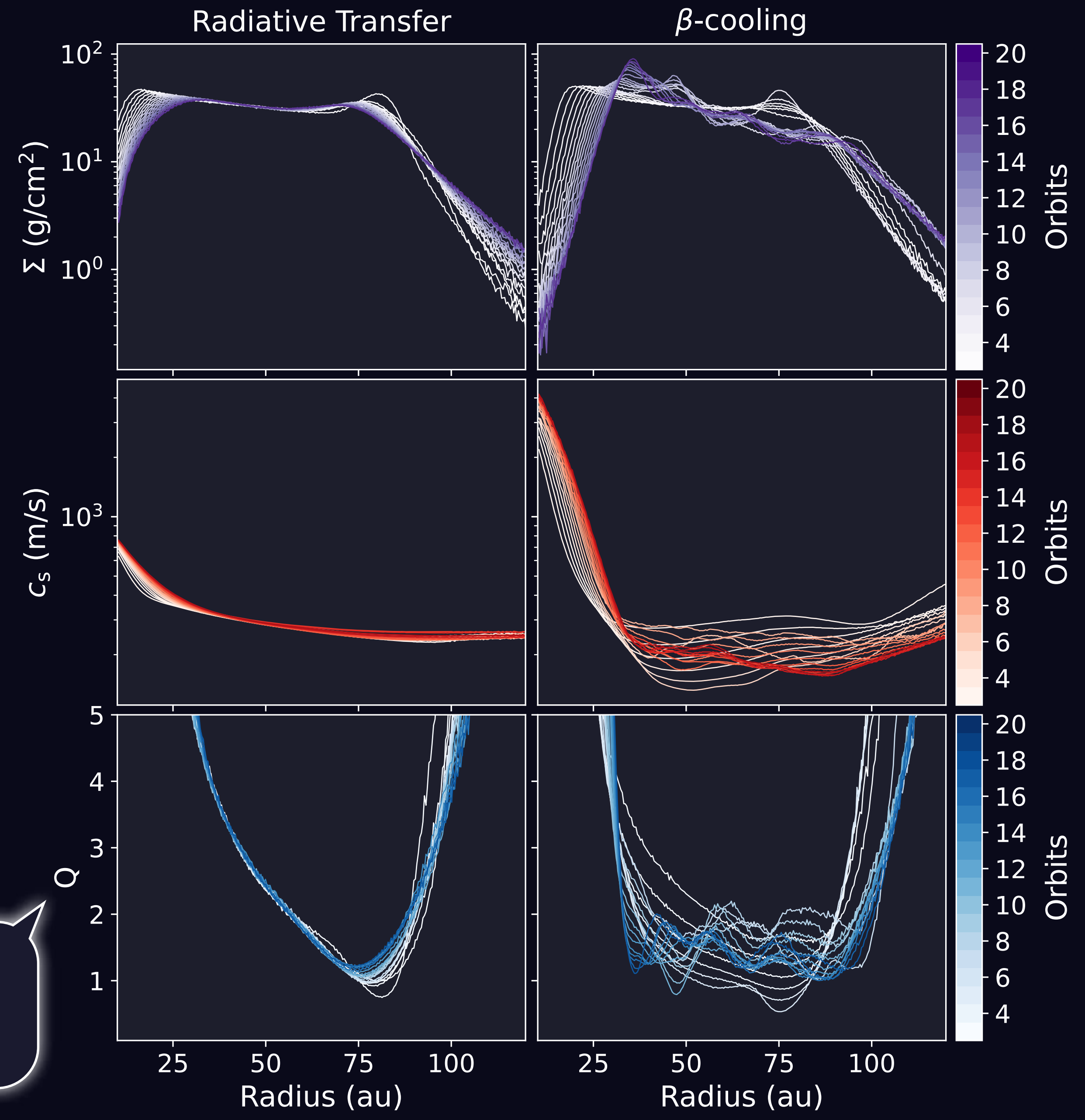


Evolution of Disc Instability

β cooling

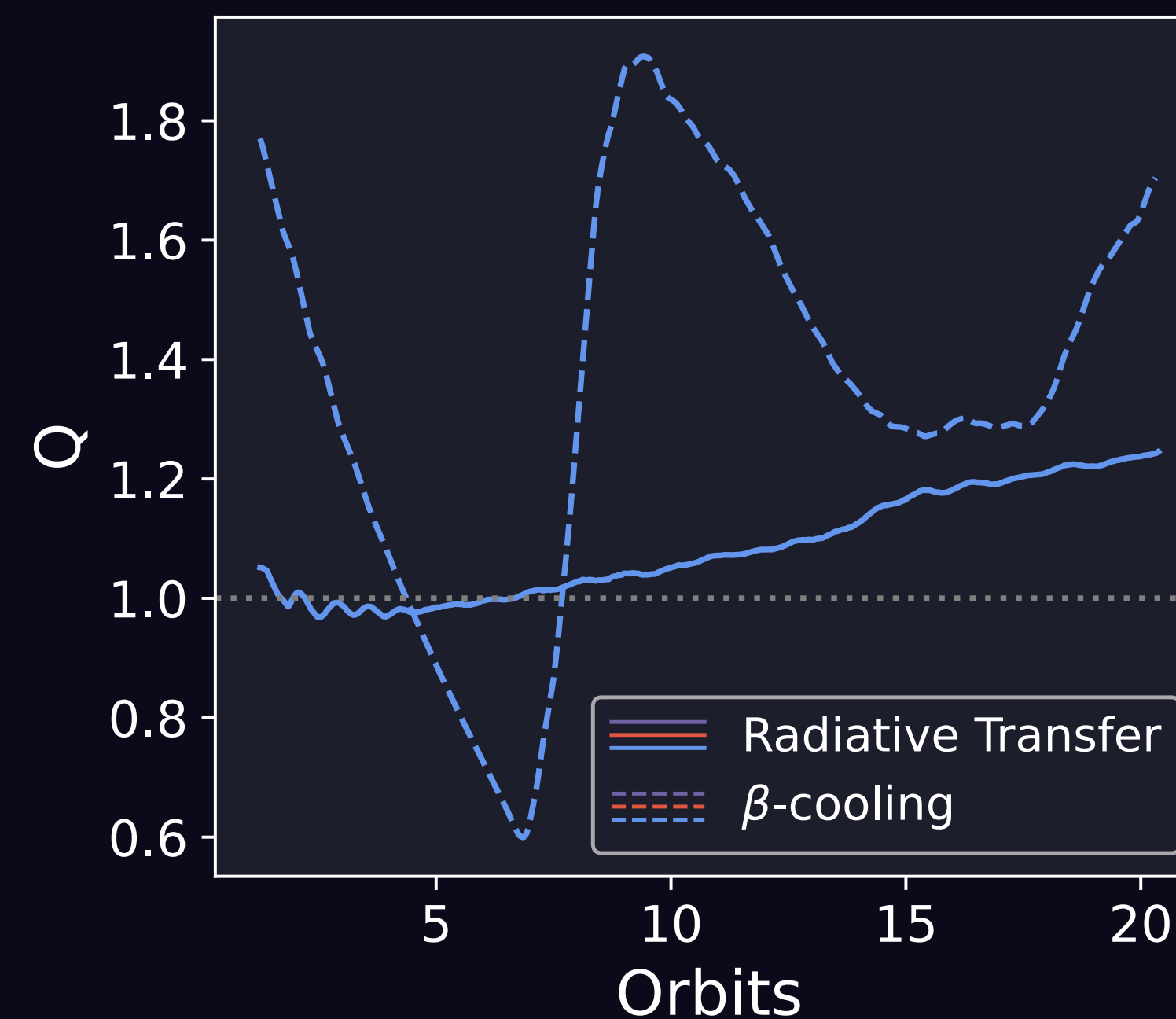
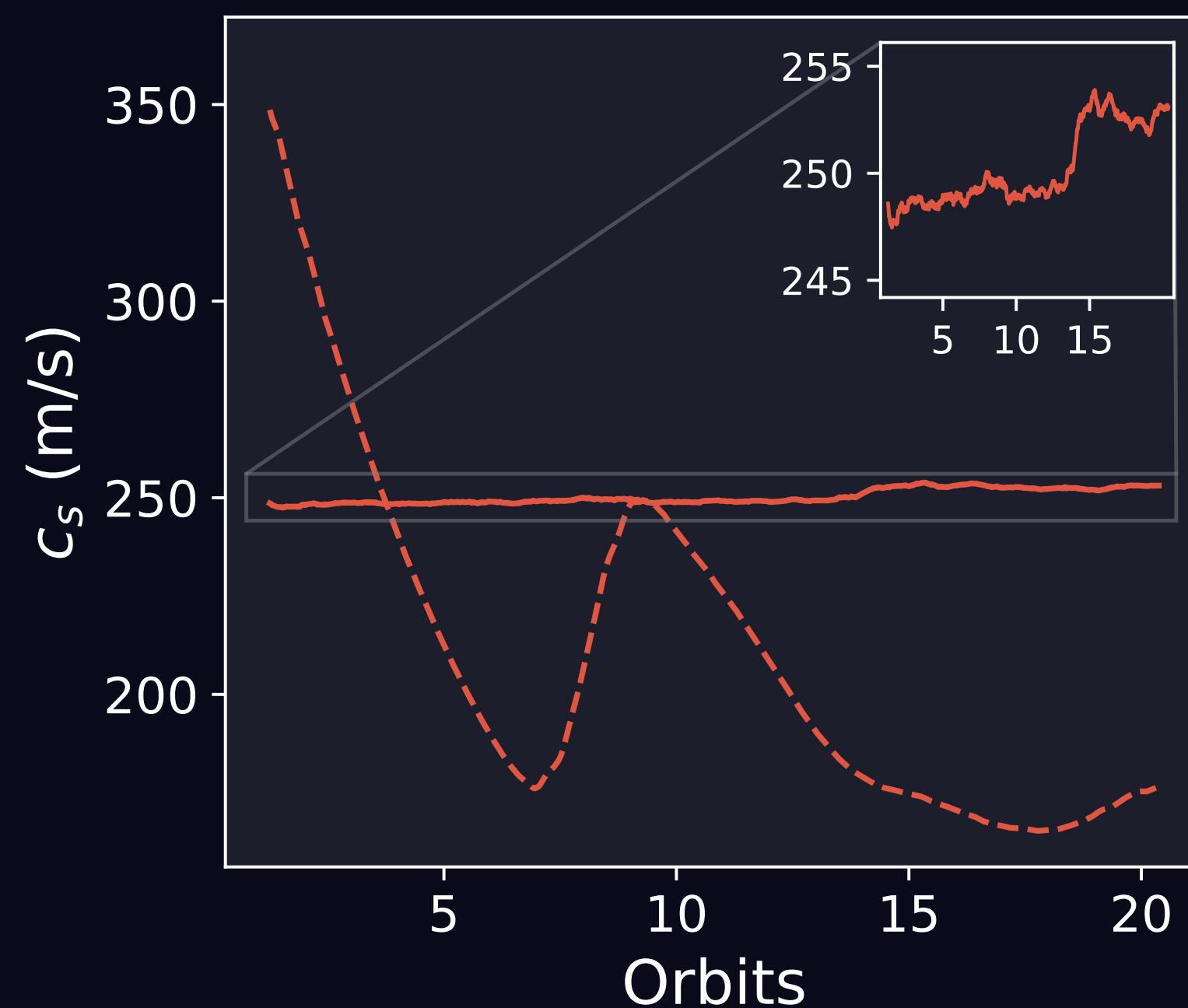
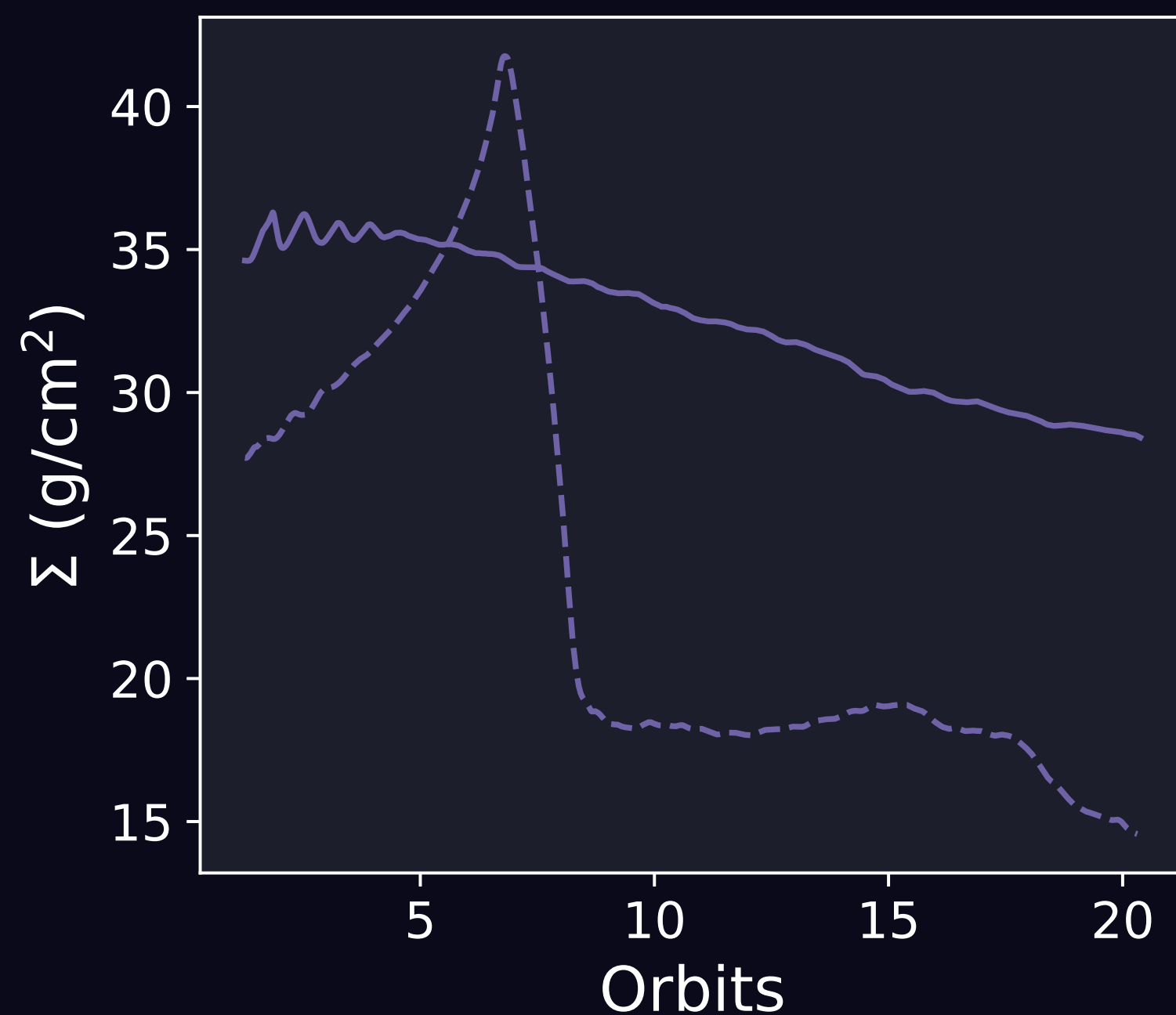
- Both surface density and sound speed evolve.
- Q eventually stabilises when heating and cooling are in balance.

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



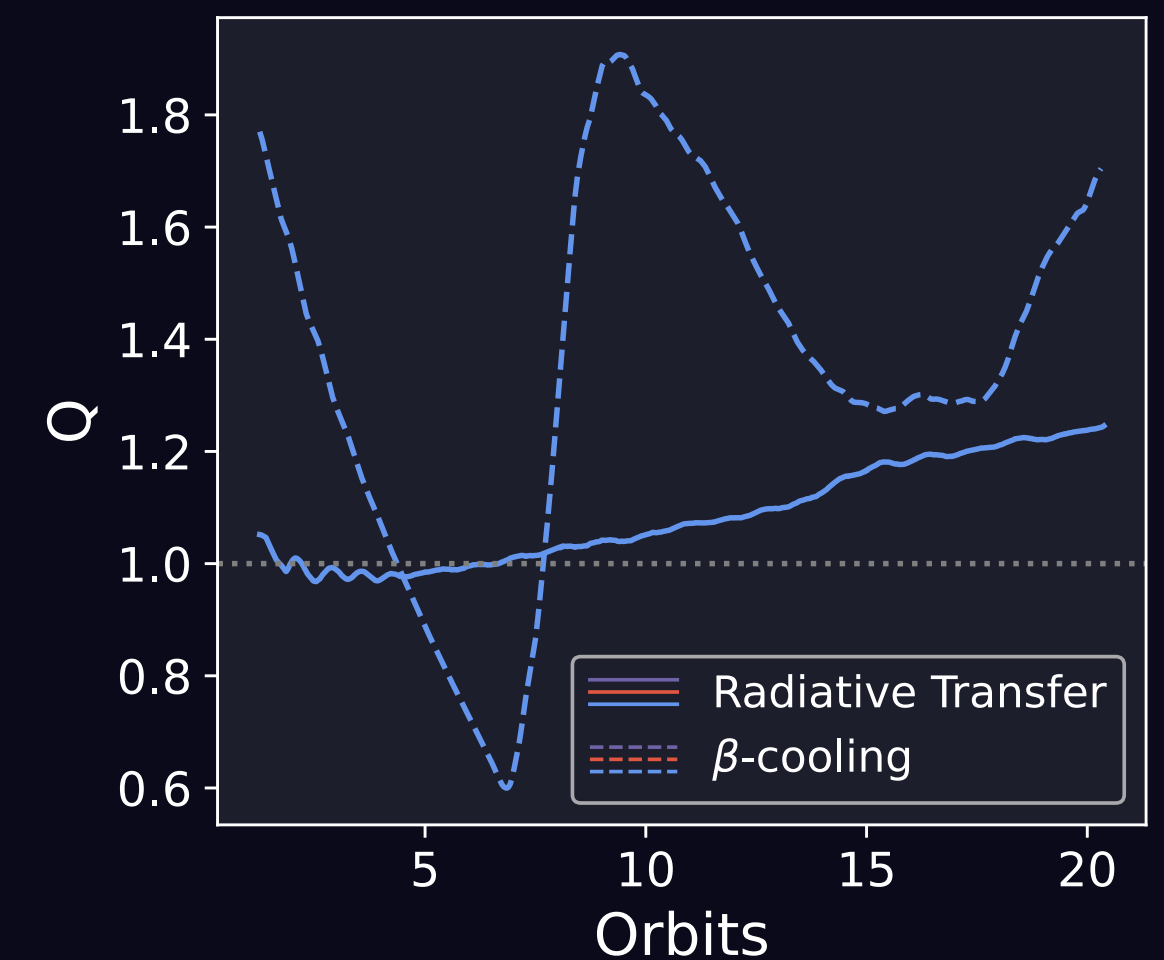
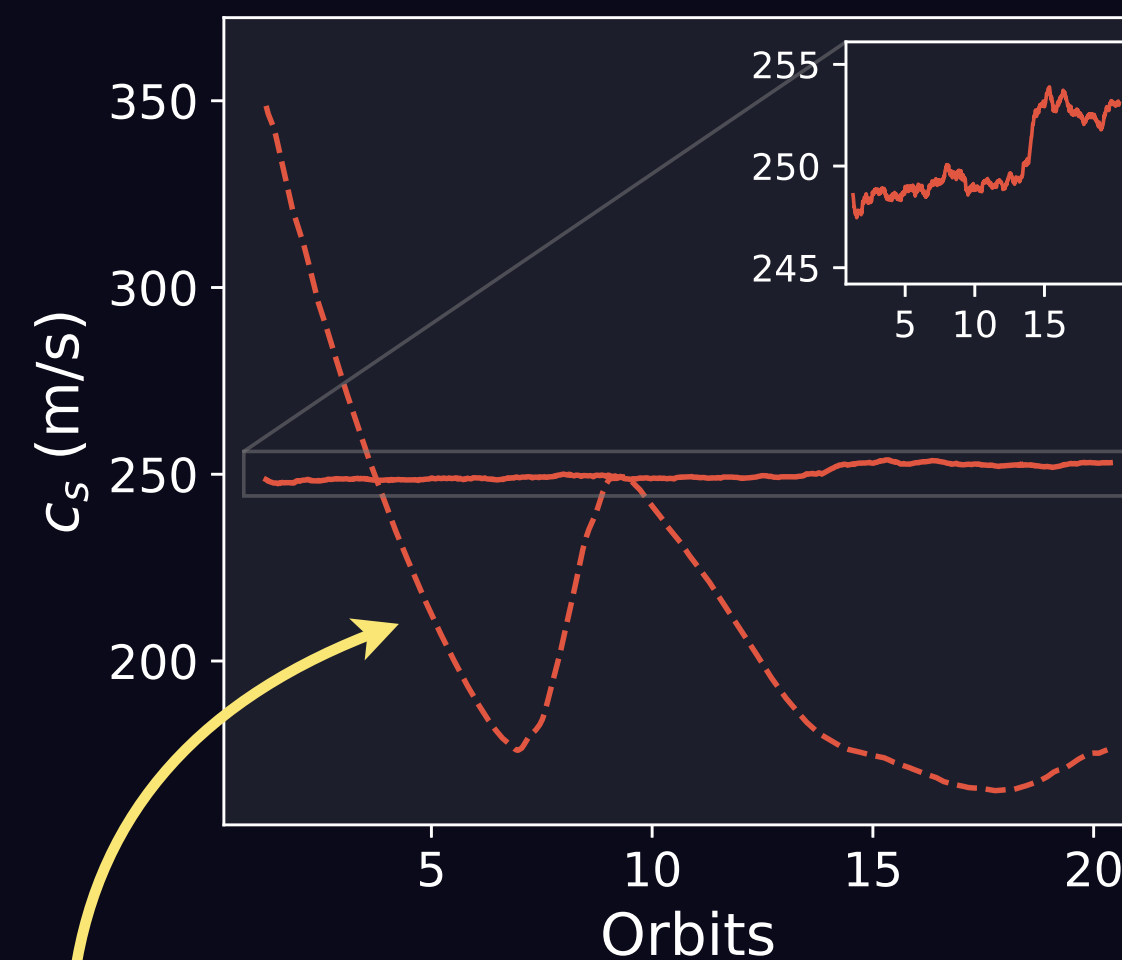
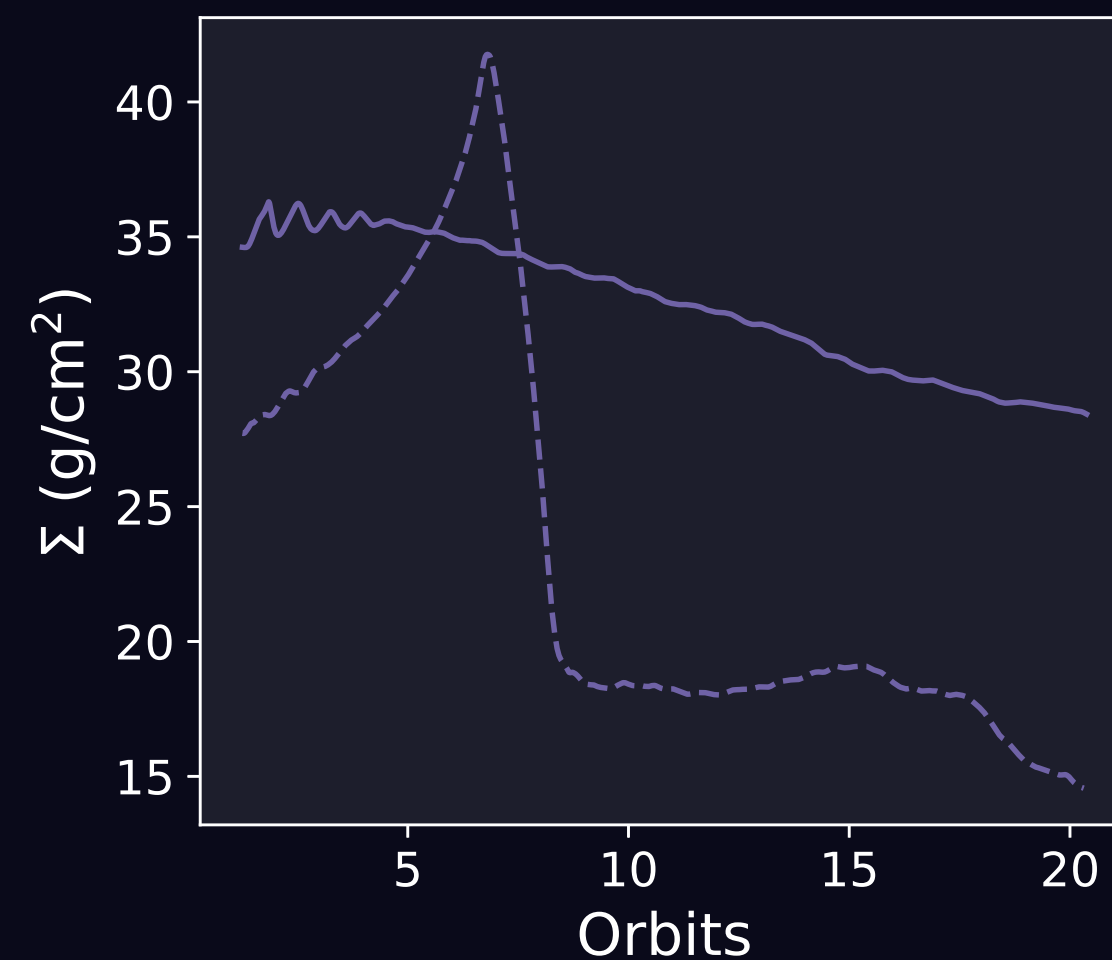
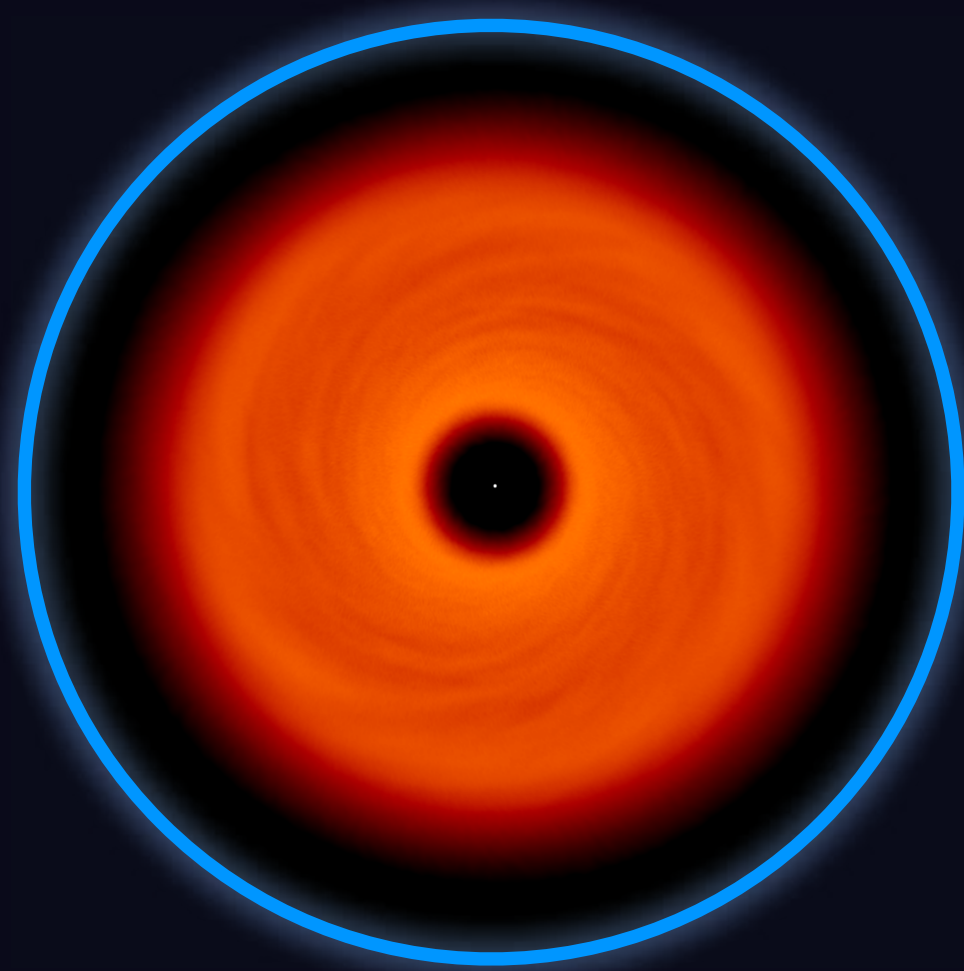
Evolution of Disc Instability (At $R=77\text{AU}$)

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



Evolution of Disc Instability (At $R=77\text{AU}$)

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

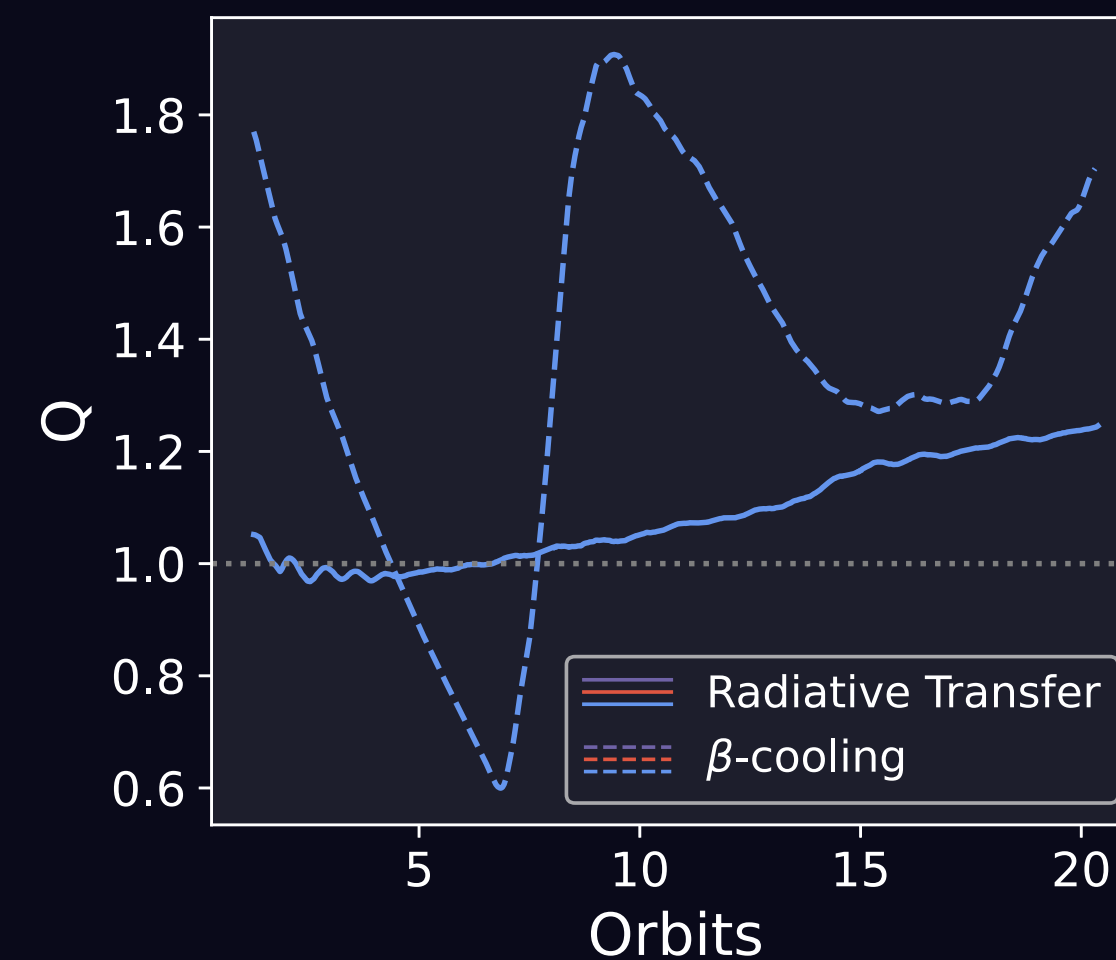
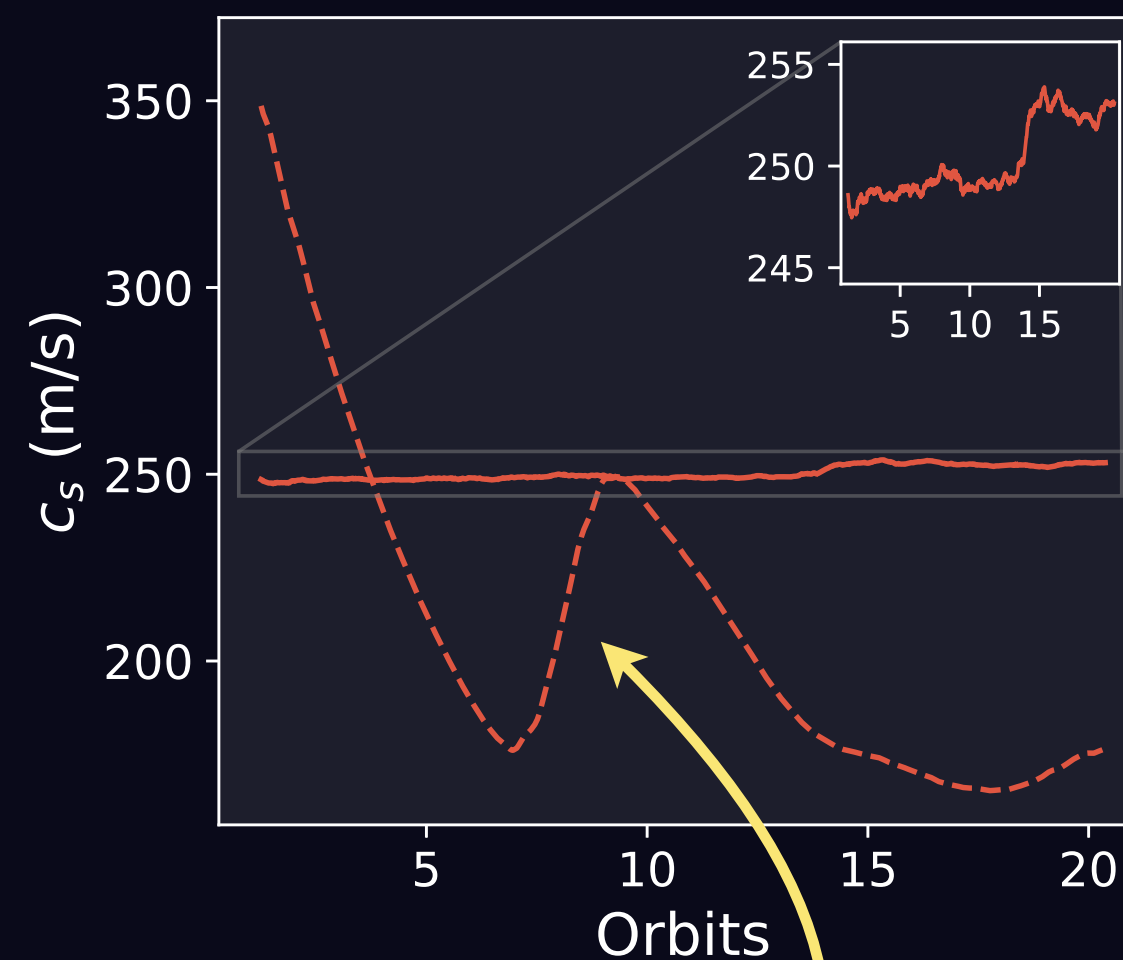
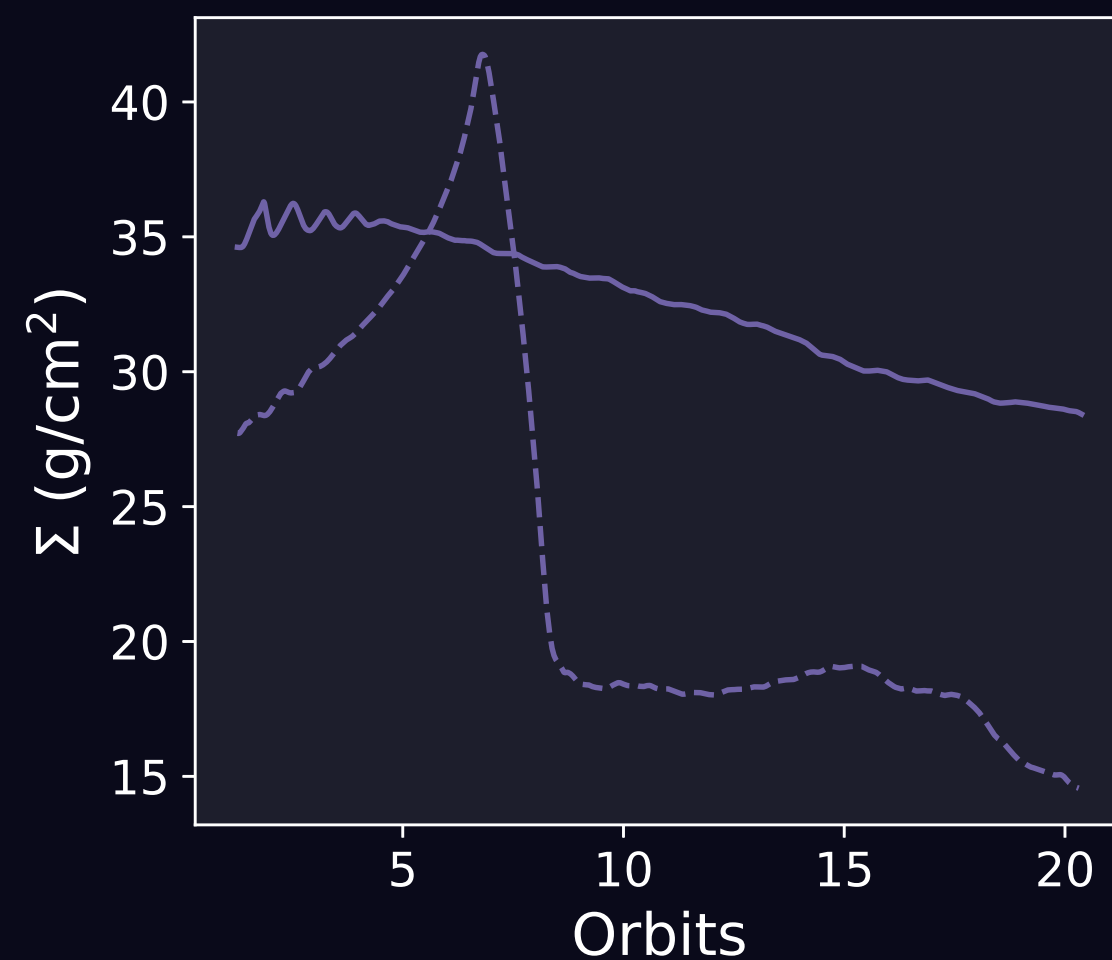
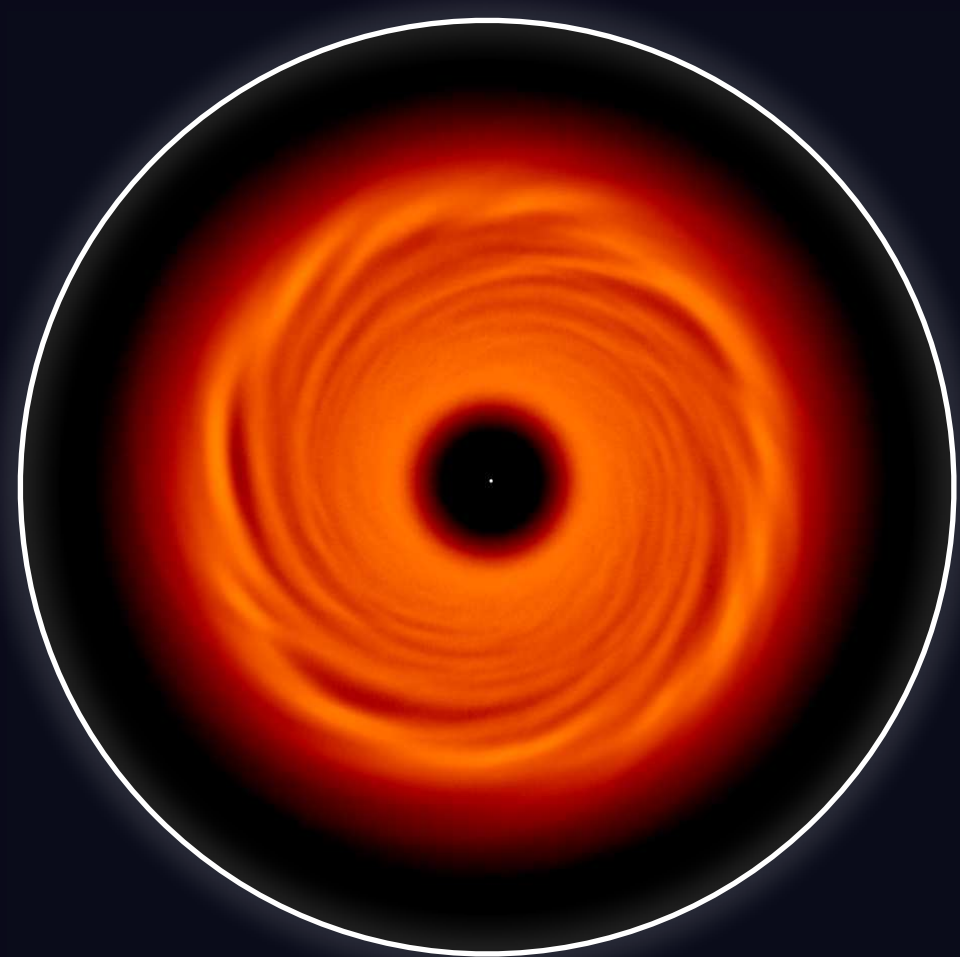


Initially, very little PdV and shock heating,
so the disc just cools.

Evolution of Disc Instability (At $R=77\text{AU}$)

Disc has cooled enough to form dense spirals.

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

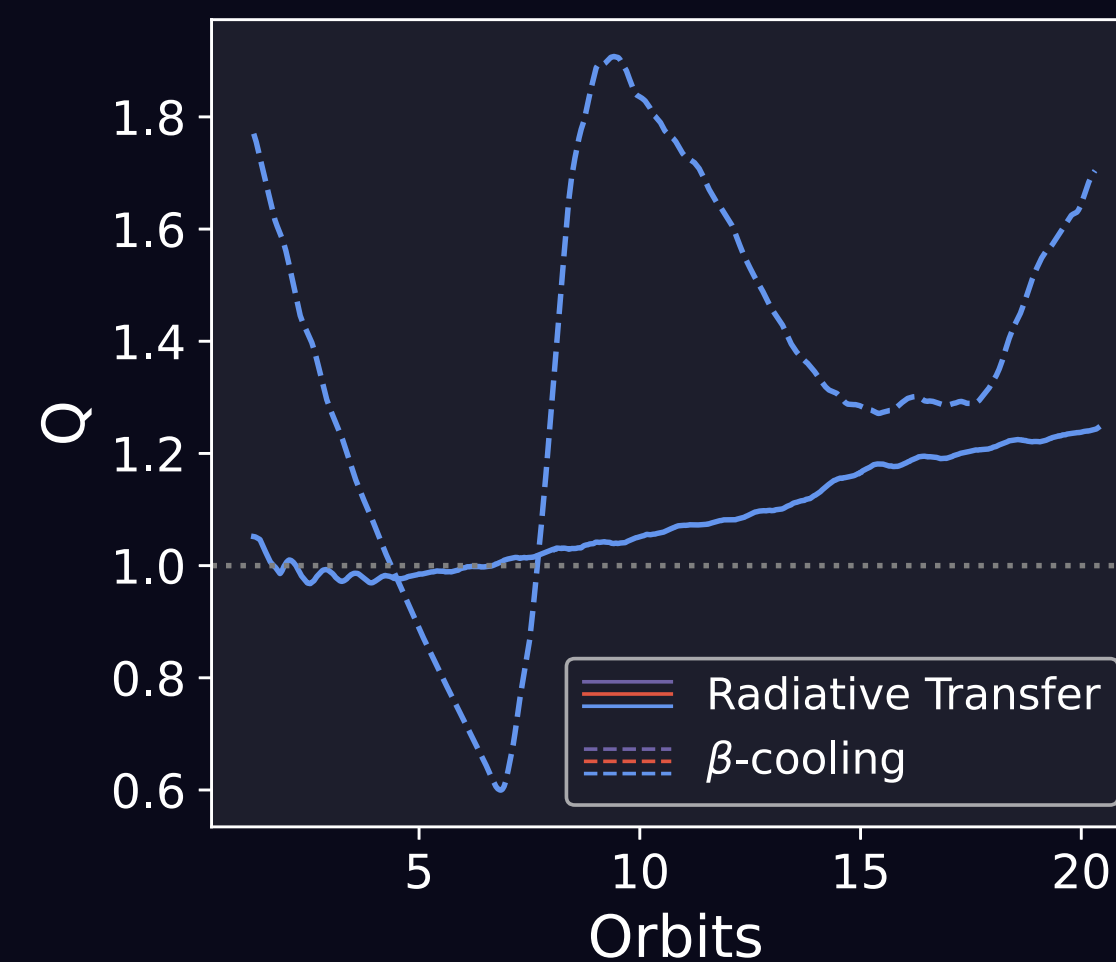
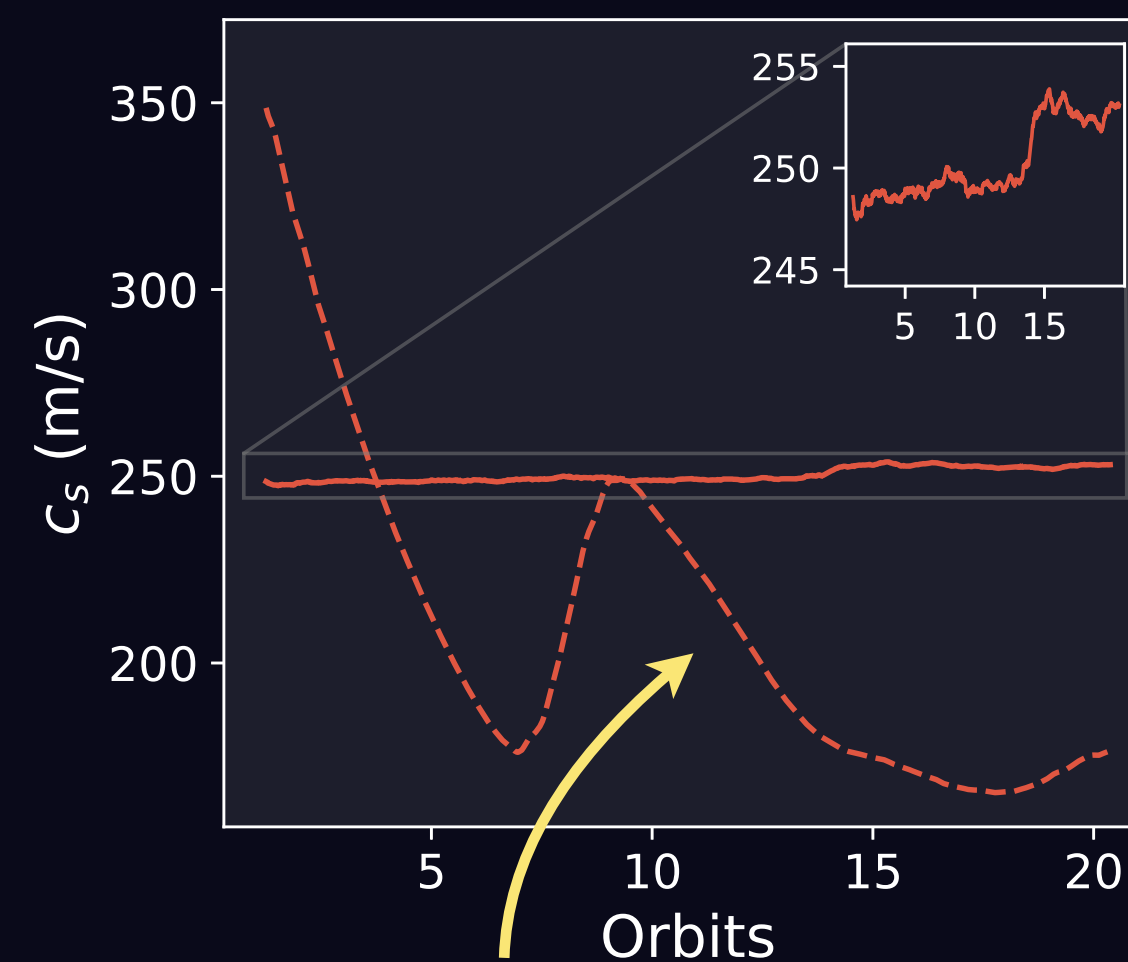
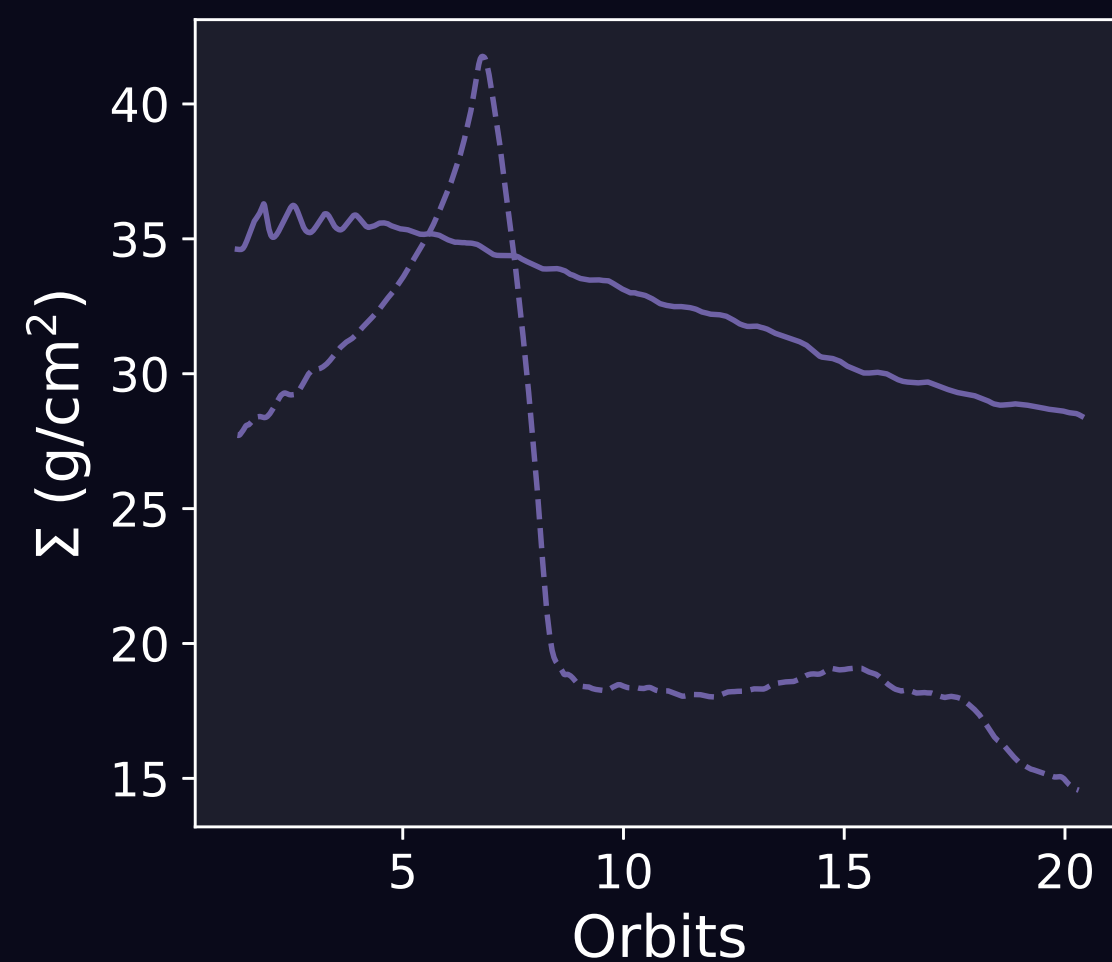
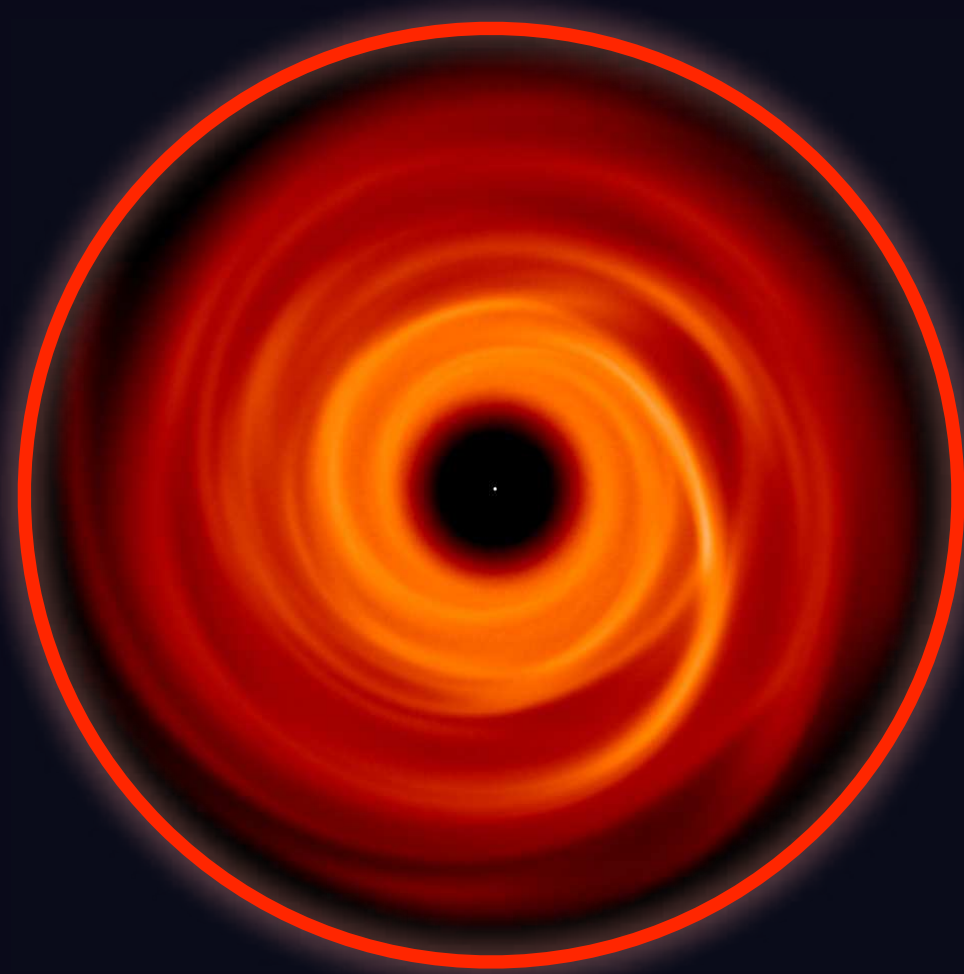


Spirals are strong enough to stabilise the disc through PdV and shock heating

Evolution of Disc Instability (At $R=77\text{AU}$)

Spirals weaken as the disc heats up.

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

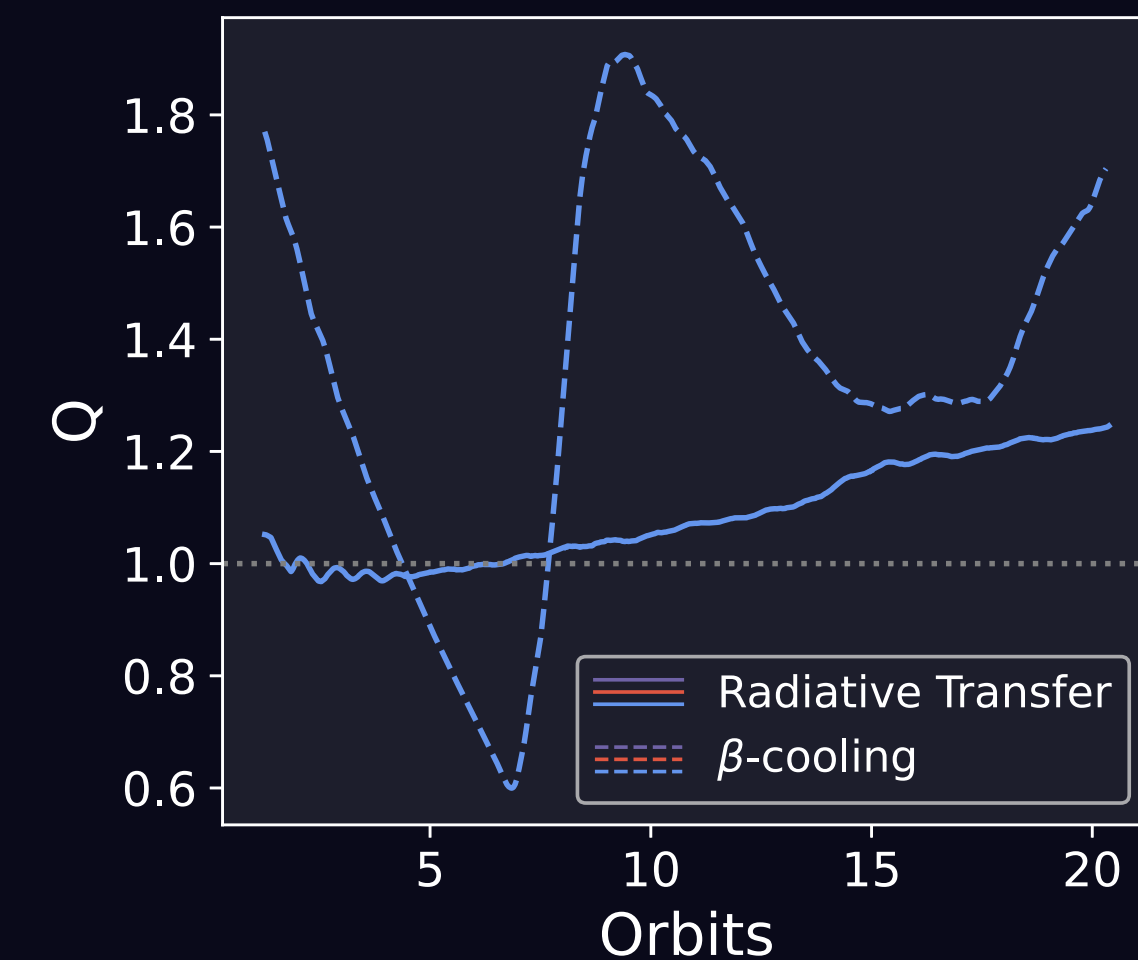
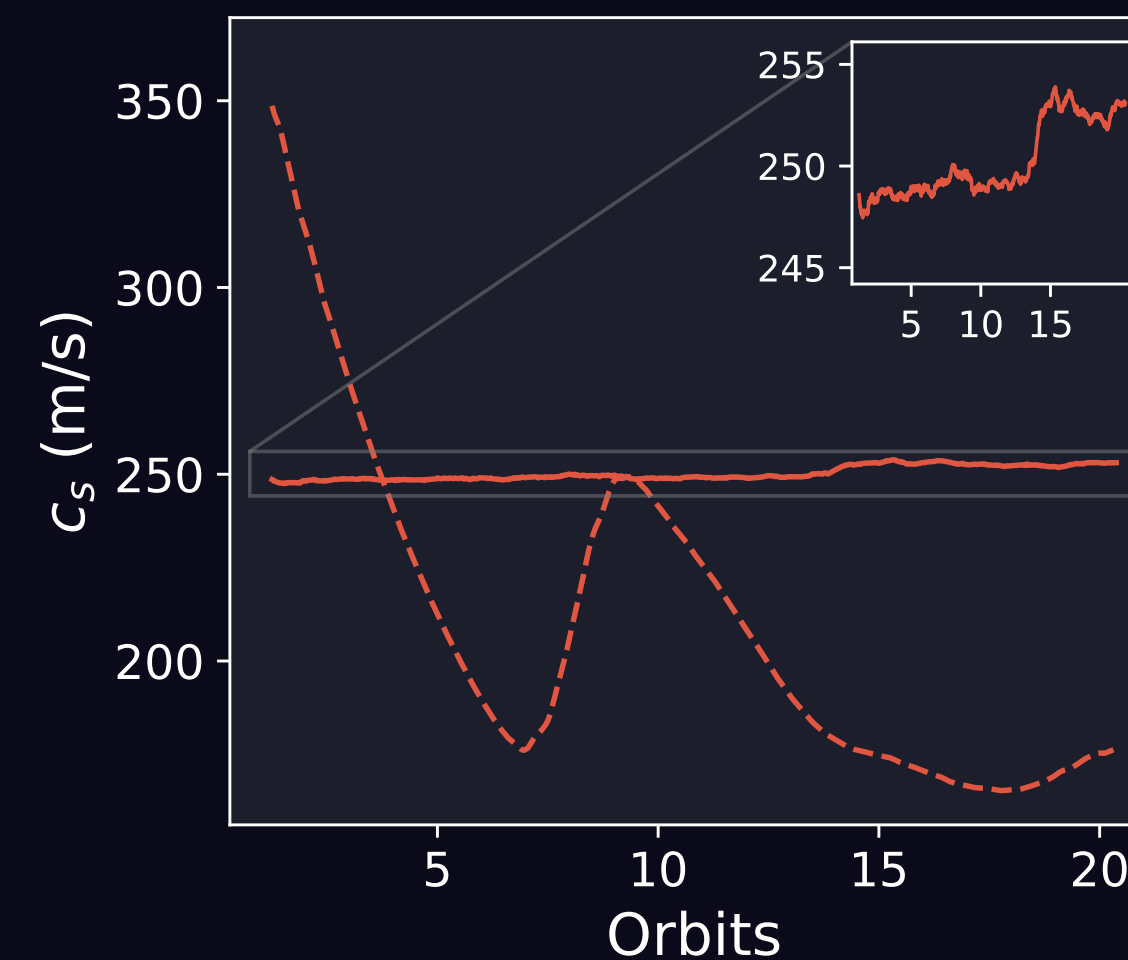
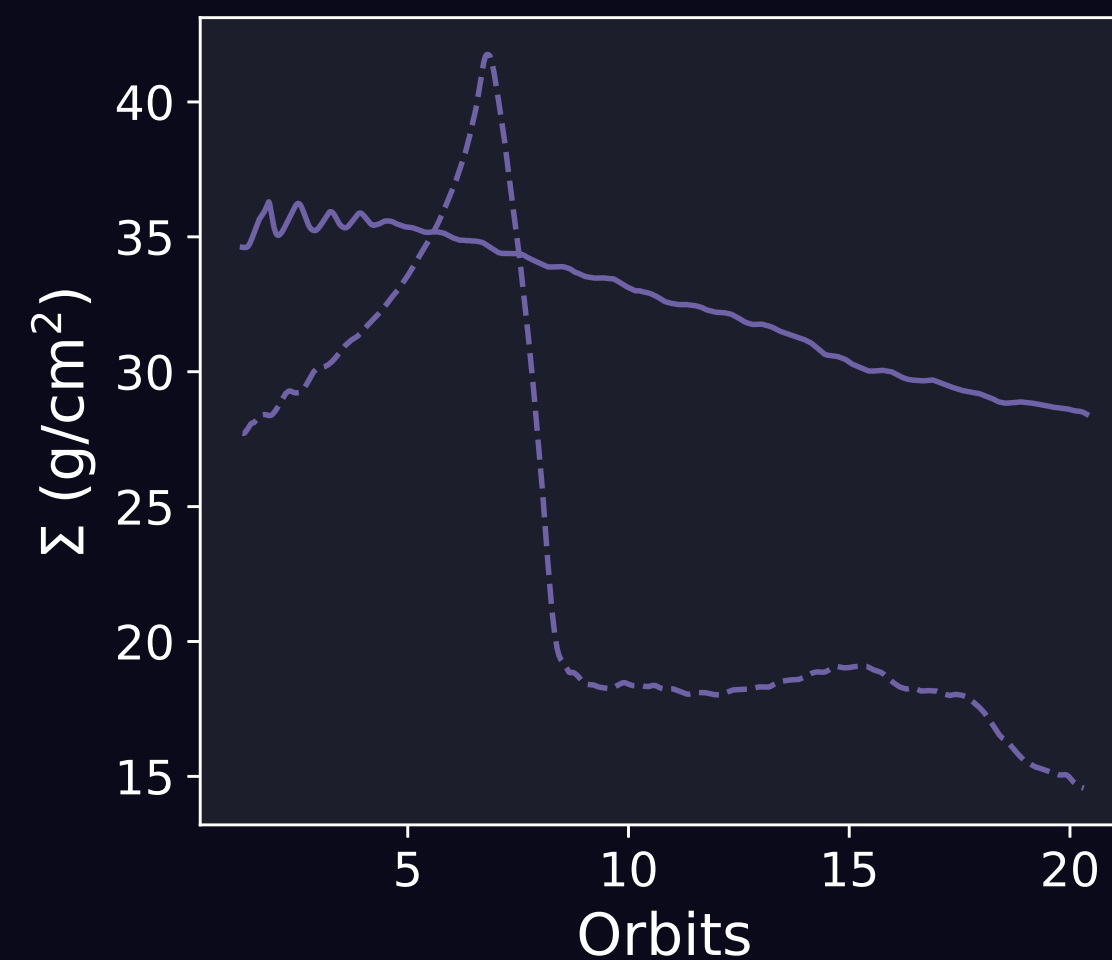


Cooling takes over once more as PdV and shock heating lessen

Evolution of Disc Instability (At $R=77\text{AU}$)

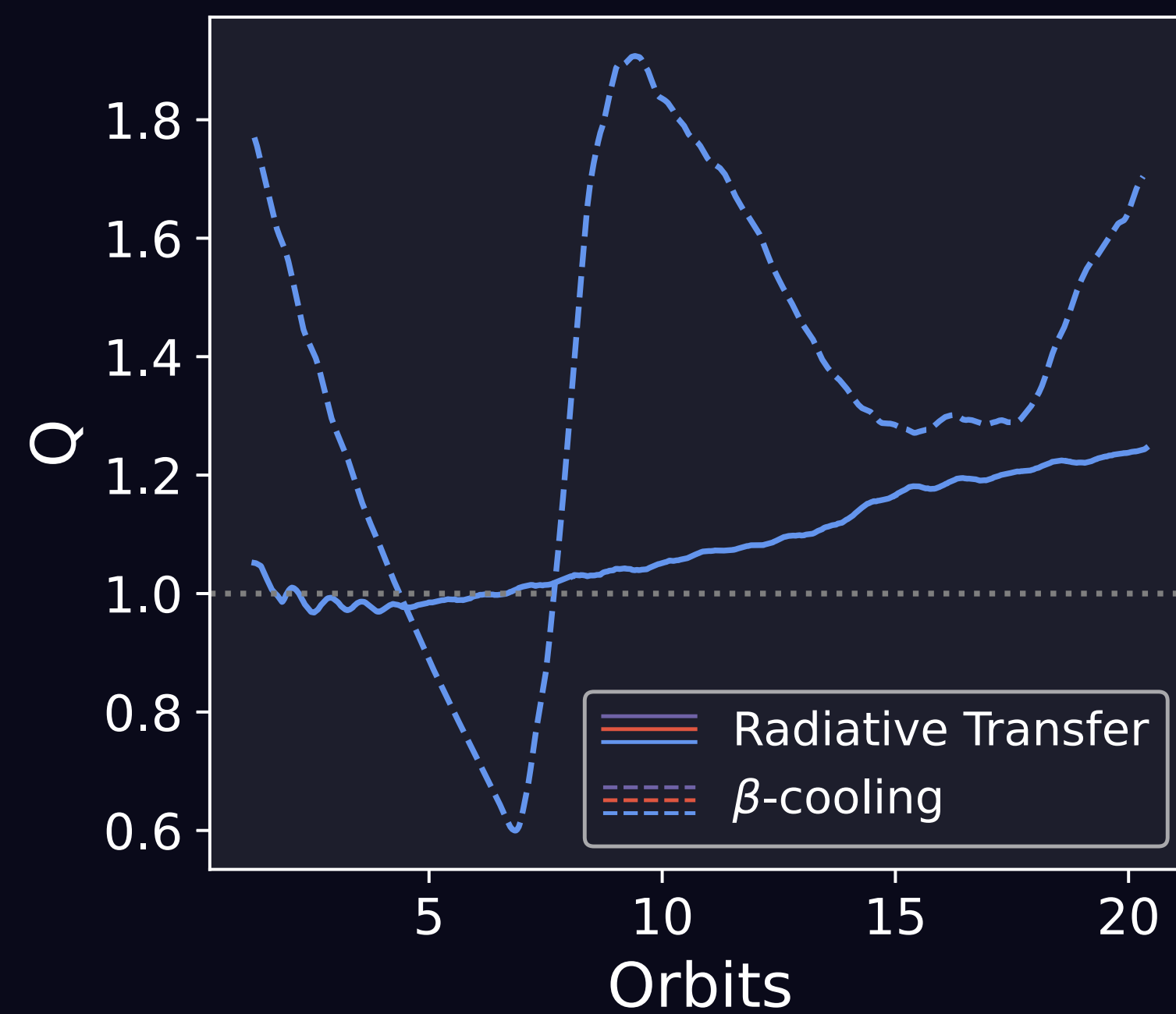
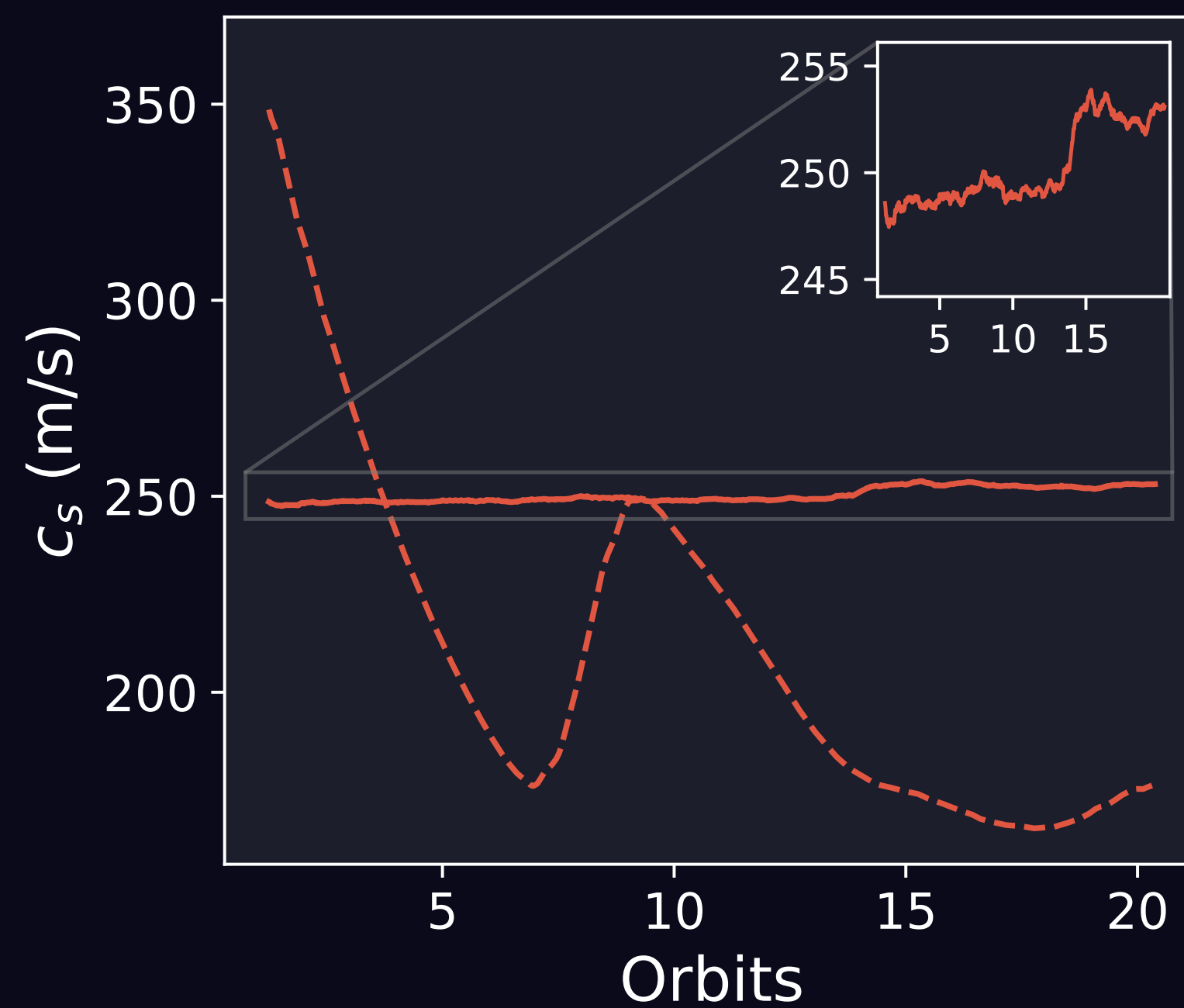
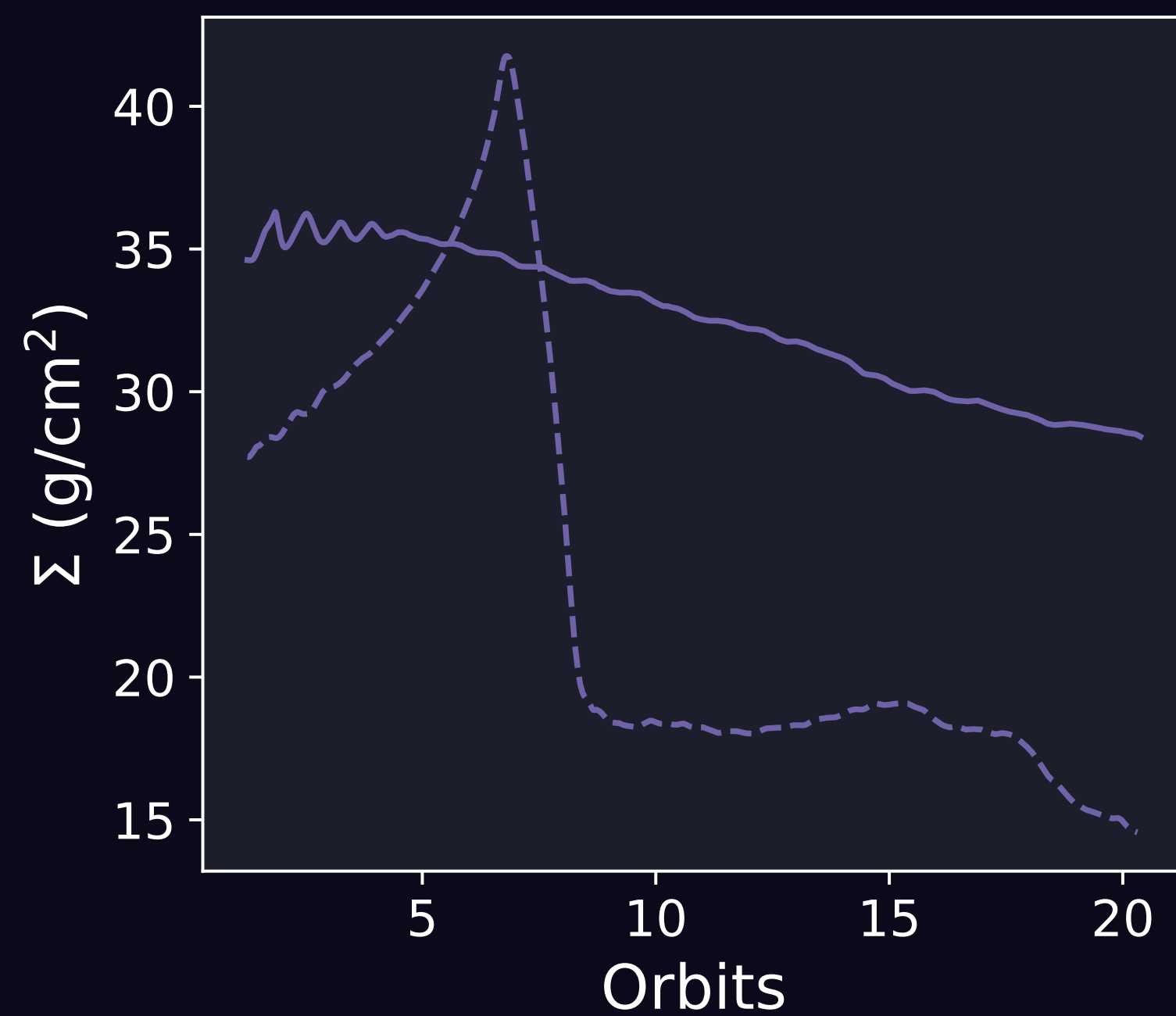
Steady spiral structures as cooling is balanced by PdV and shock heating

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



Evolution of Disc Instability (At $R=77\text{AU}$)

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

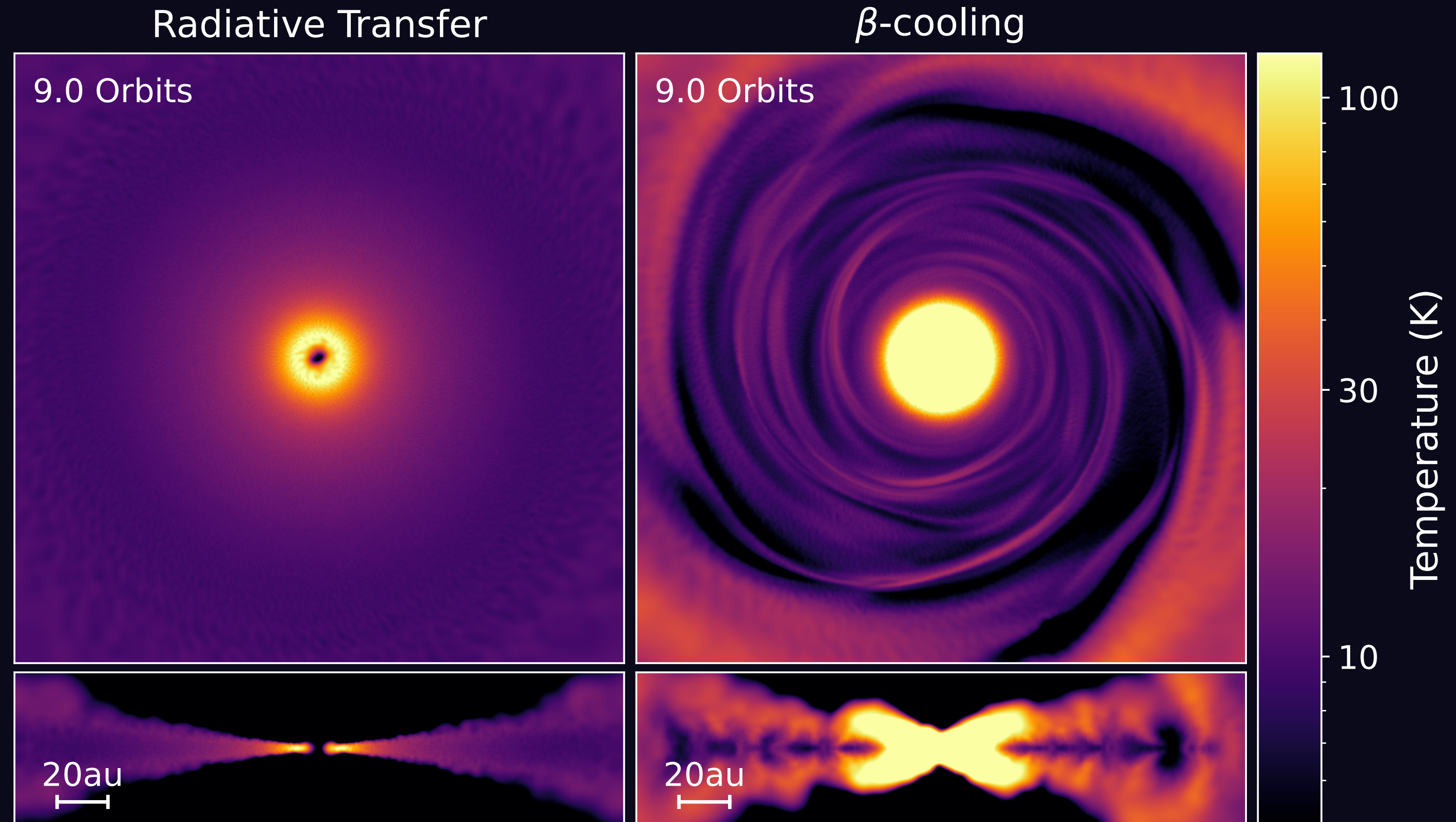


***WHY IS PdV AND SHOCK HEATING MORE
IMPORTANT FOR β COOLING?***

Temperature Structure

β cooling

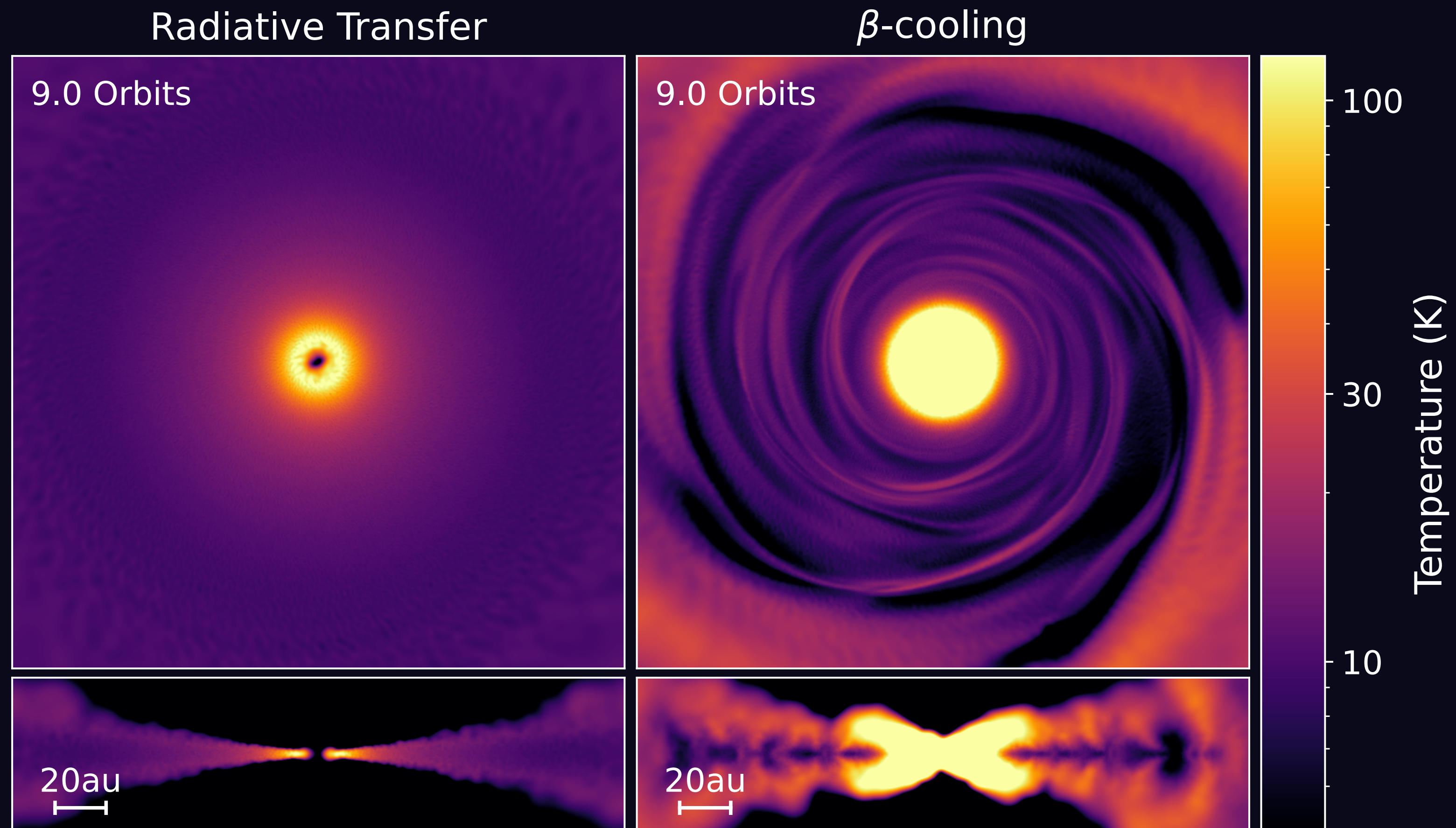
- A colder disc.
- PdV and shock heating from the spirals are the source of heating.



Temperature Structure

Radiative Transfer

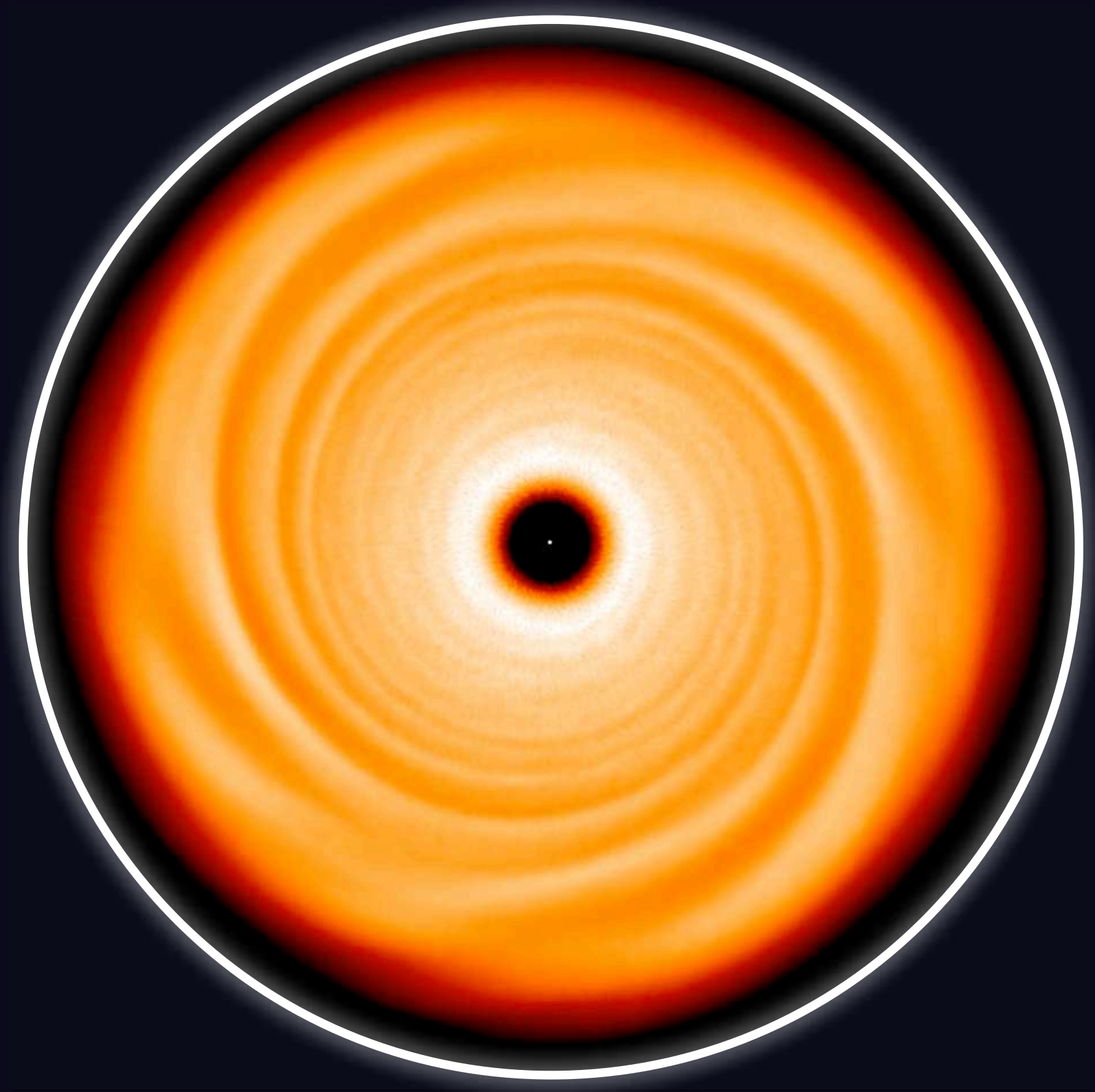
- *Disc is warmer.*
- *Stellar irradiation is the dominant source of heating.*



The Computational Cost

Radiative Transfer - $3e8$ CPU seconds

β cooling - $3e6$ CPU seconds

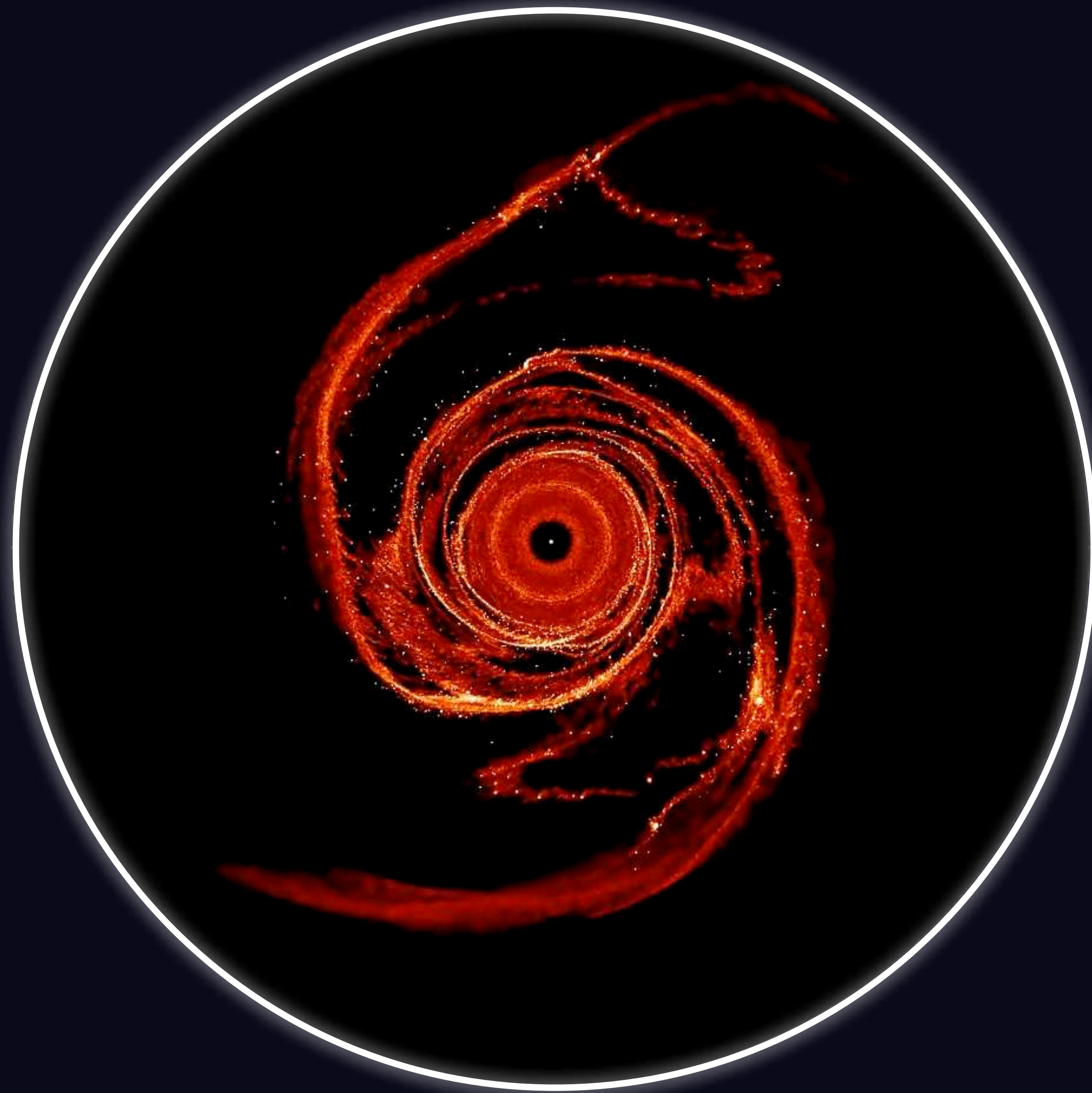


WHY BOTHER SIMULATING FOR MONTHS?



Dust Dynamics

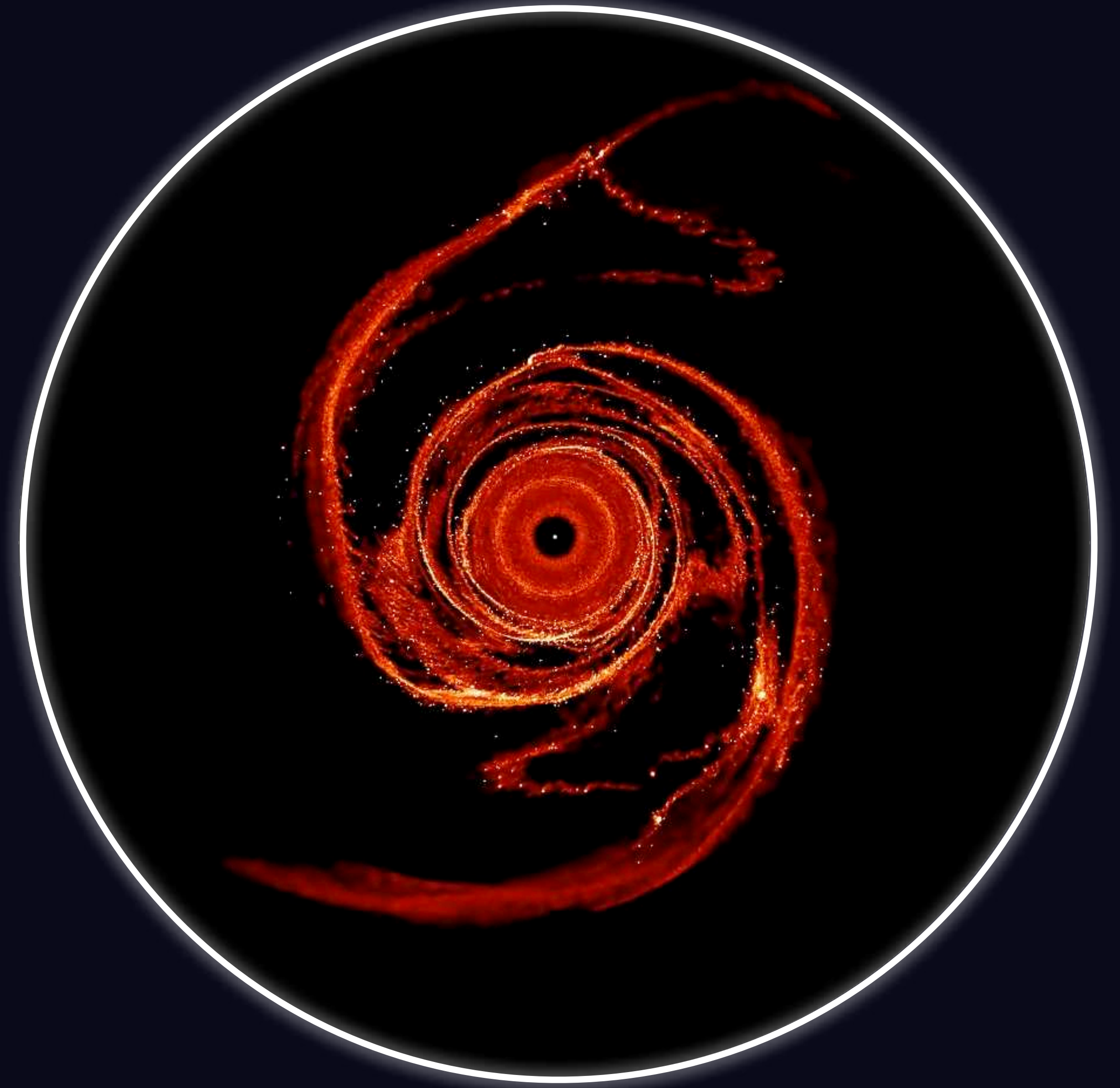
- *The spirals are regions of pressure maxima where dust can be efficiently trapped and grow to form planetesimals.*



Rowther+ 2024

Dust Dynamics

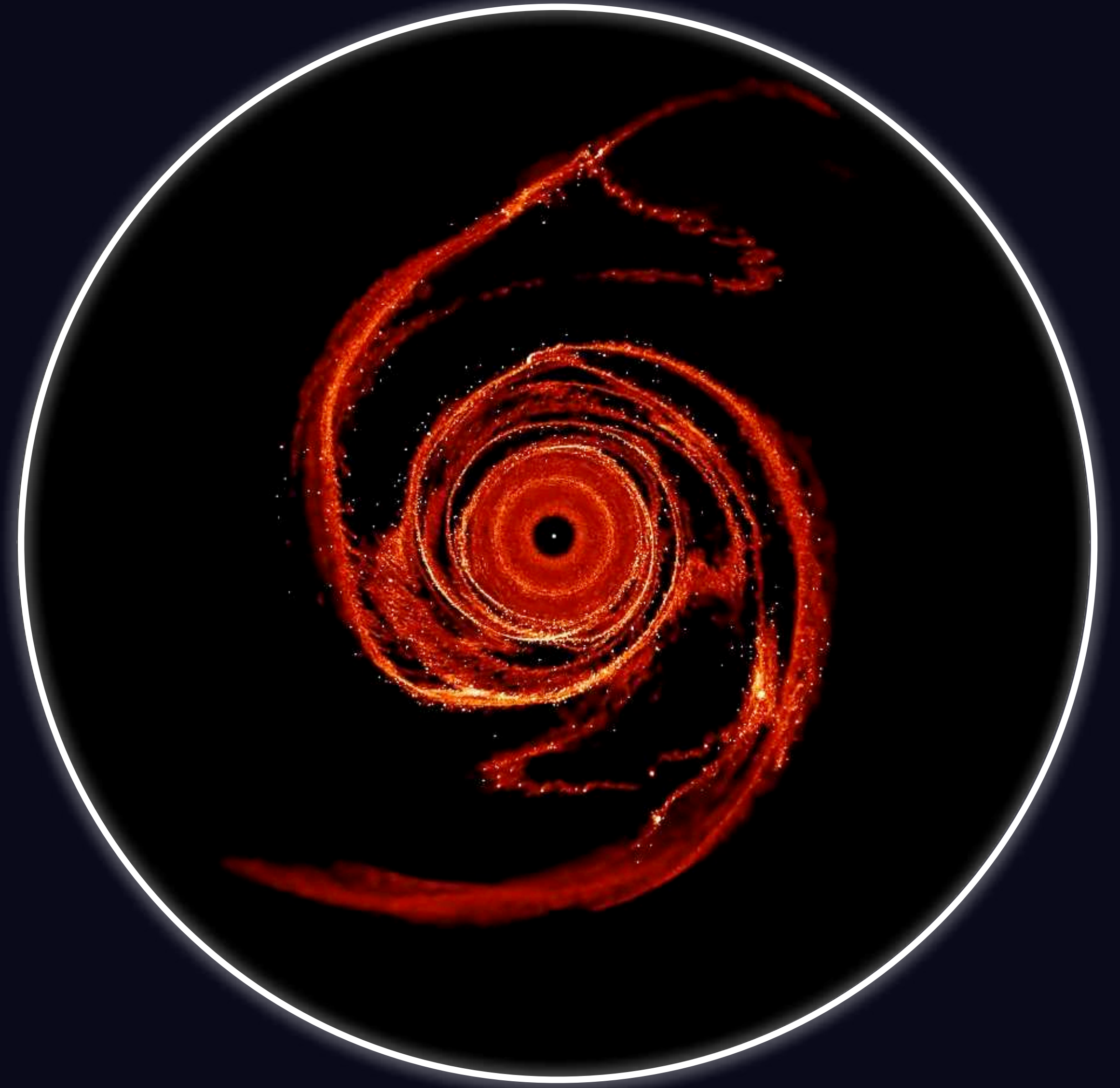
- *Dust is kicked around by high amplitude spirals (Longarini+ 2023b).*



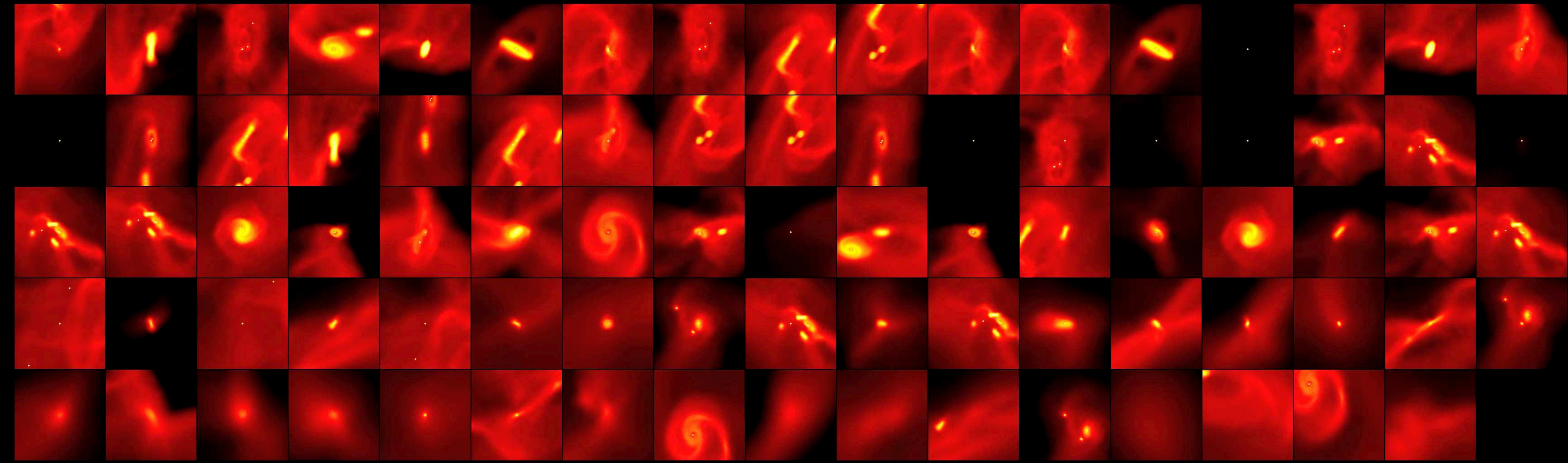
Rowther+ 2024

Dust Dynamics

- *The weaker spirals with radiative transfer could be more favourable to forming planetesimals.*



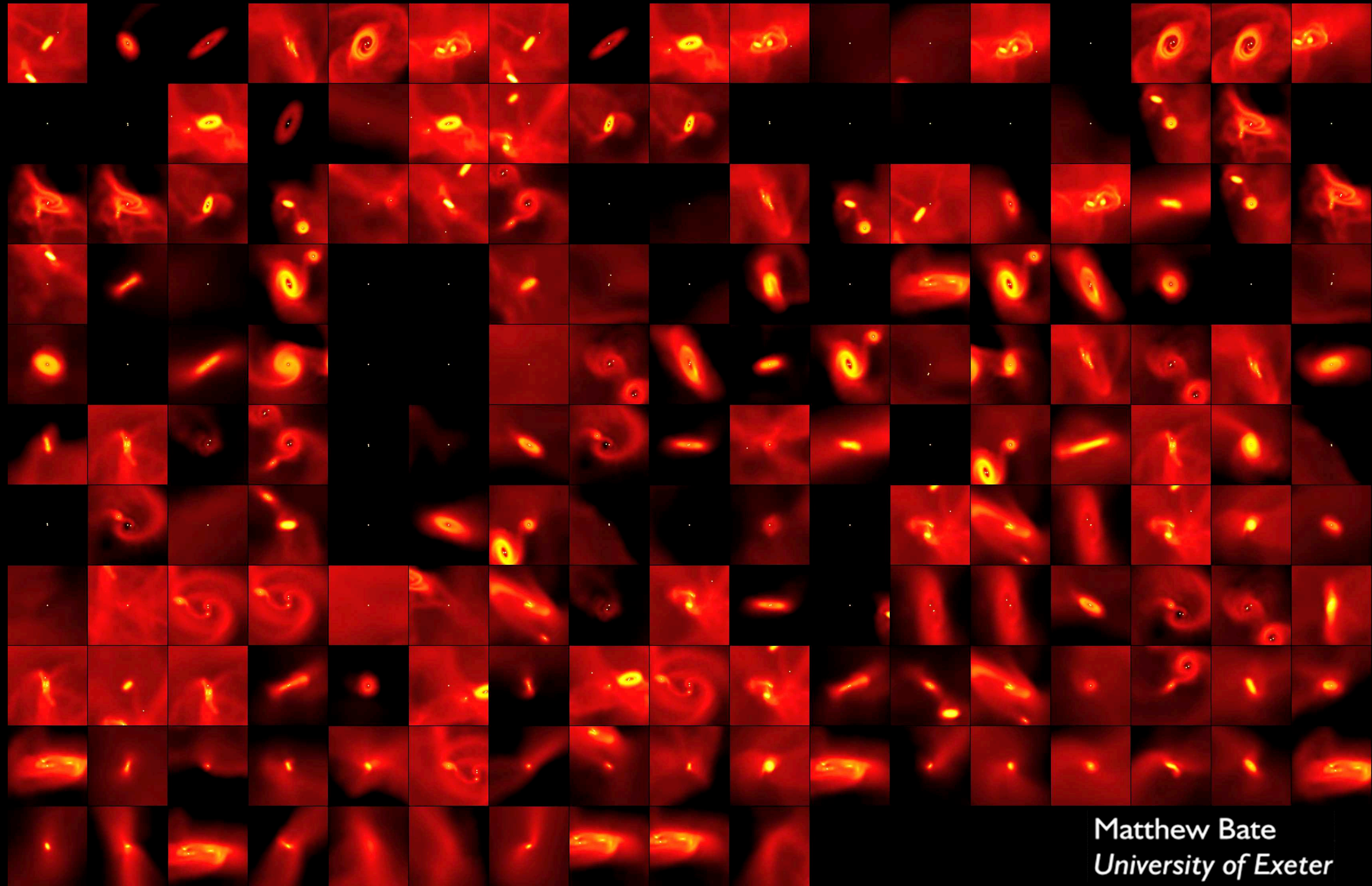
Rowther+ 2024



*Discs do
not evolve
in isolation*

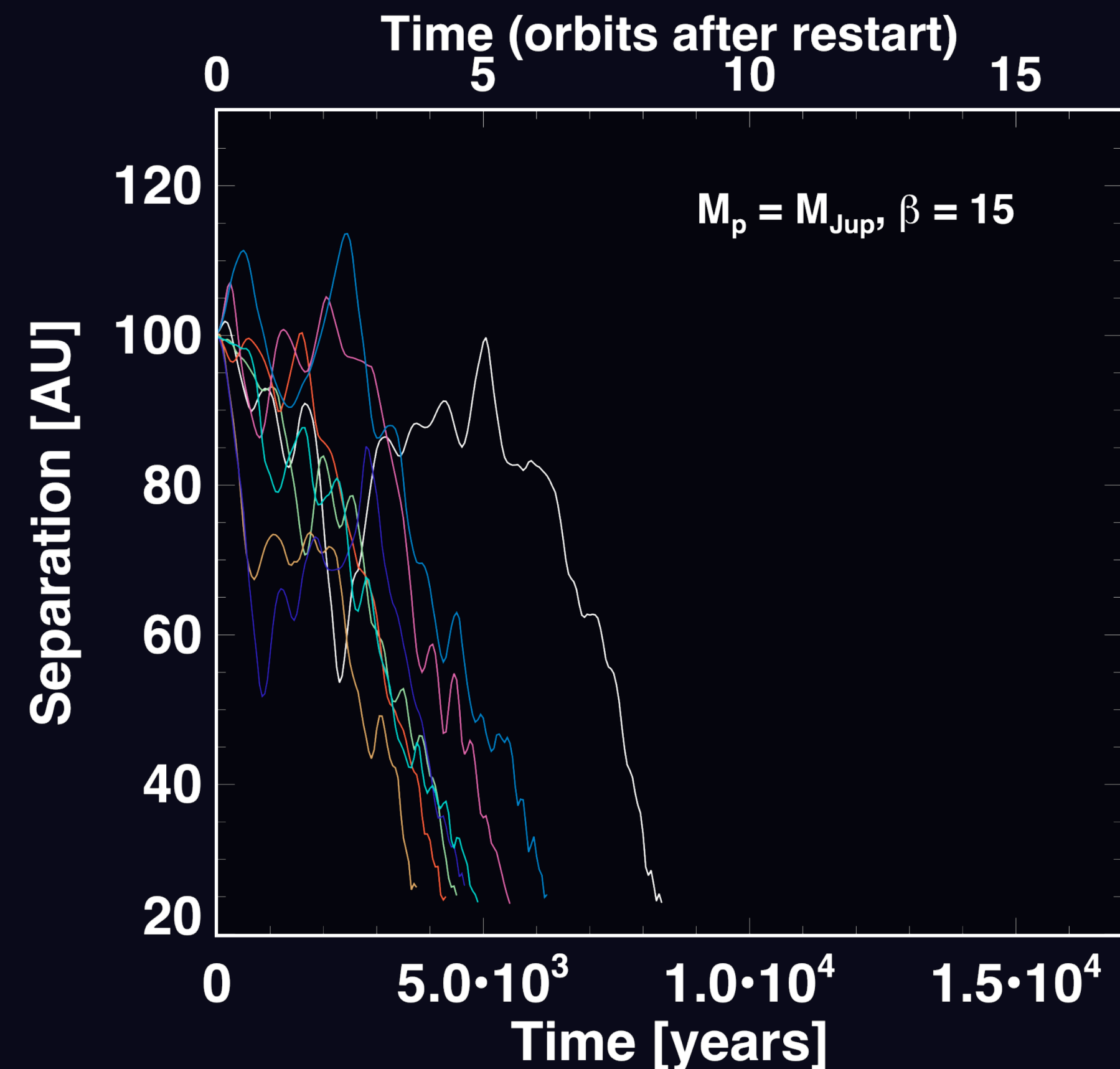
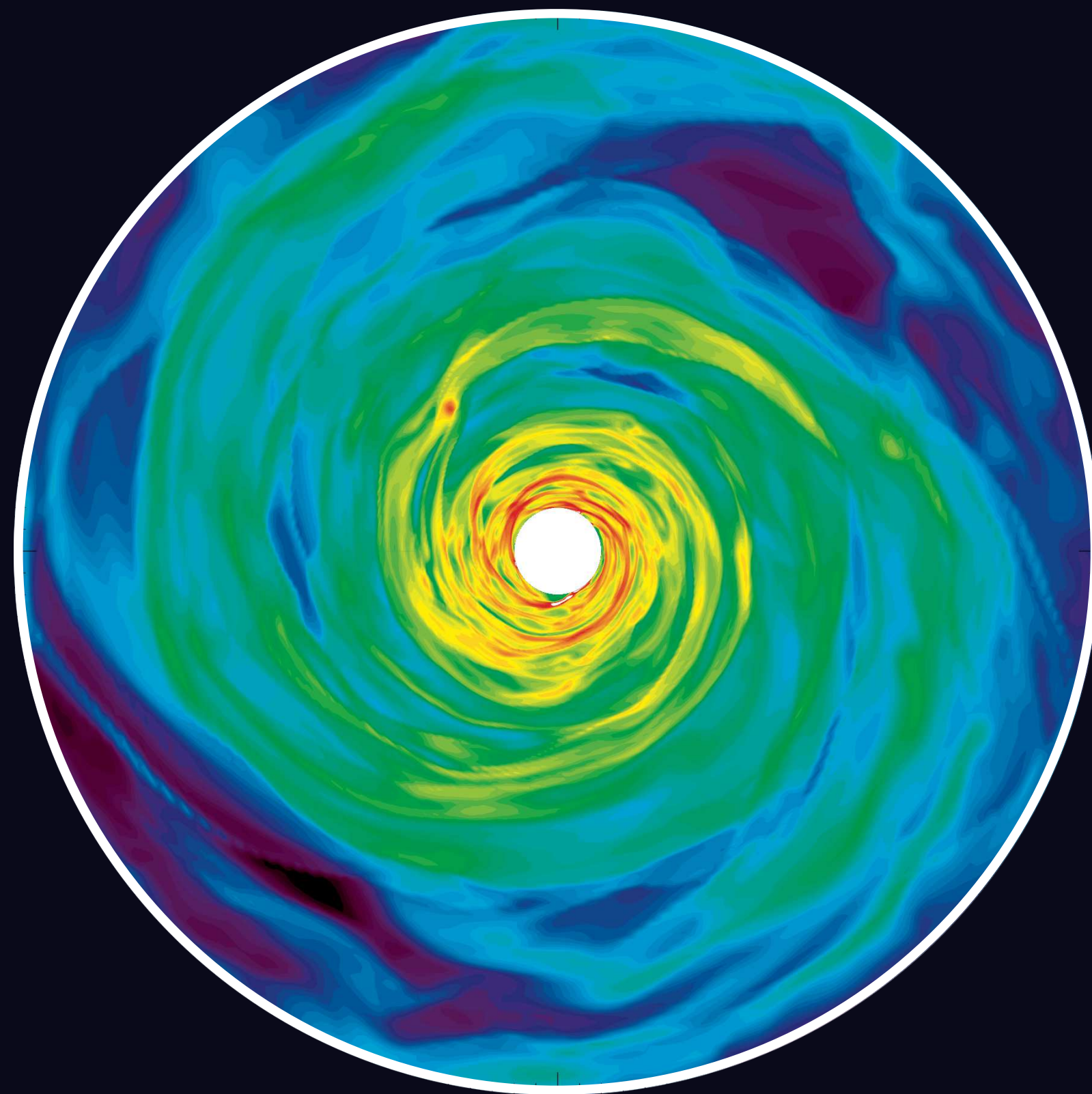
Matthew Bate
University of Exeter

*Neighbours,
companions, and
chaotic accretion
episodes all can
alter the evolution
of the disc*



Matthew Bate
University of Exeter

The Doom of Giant Planets

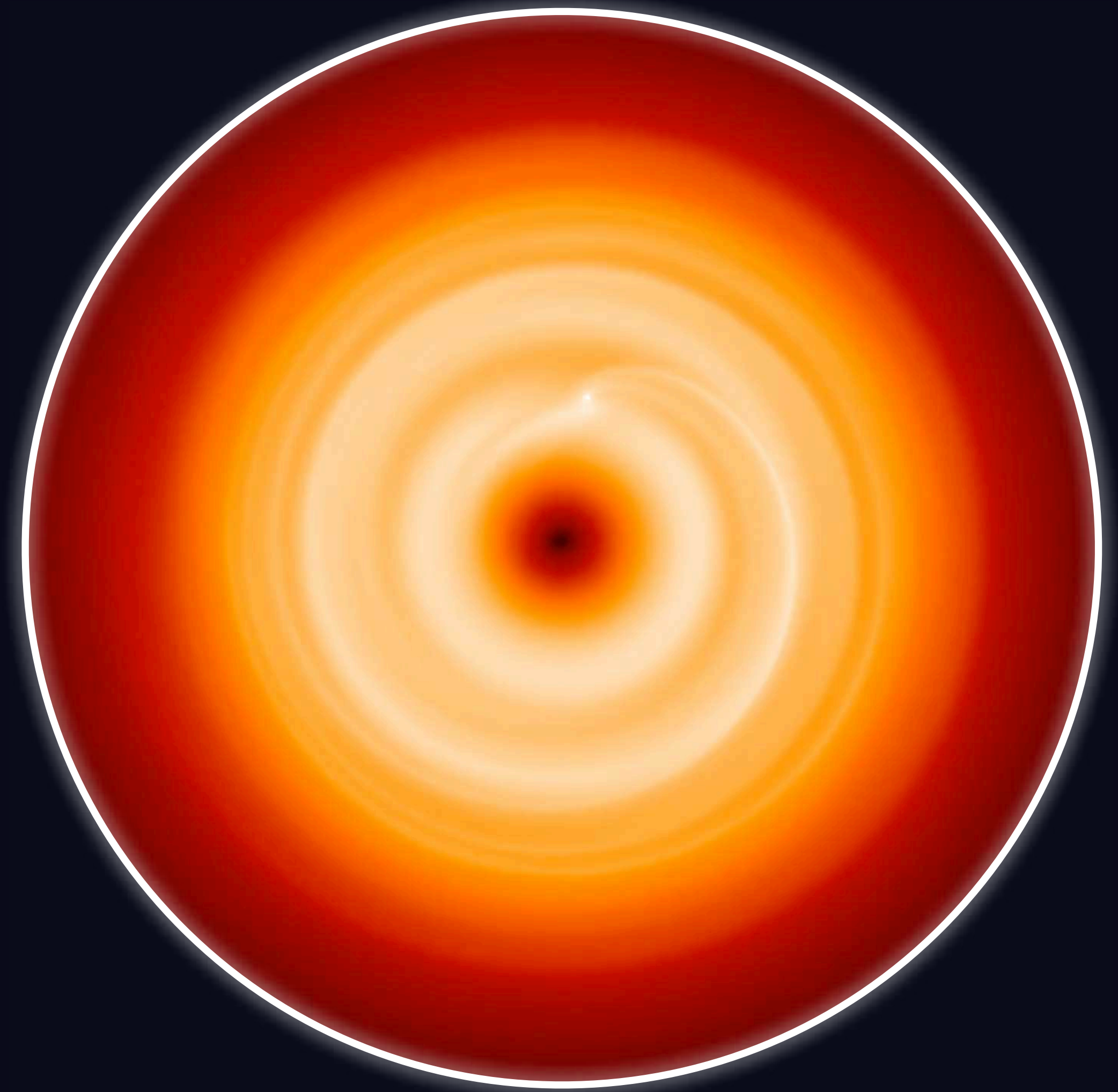


Planets migrate inwards rapidly within a few orbits in discs modelled with simple thermodynamics (Baruteau+ 2011)

Slightly better β cooling

Survival of Giant Planets

- *Spirals with radiative transfer are weaker.*
- *Could be easier for planets to open up gaps, slowing their migration.*



Rowther+ 2020, 2023

Conclusions

- *Discs can become gravitationally unstable with stellar irradiation.*
- *The contribution from PdV and shock heating is tiny. the temperature of the disc is instead set by the star, and is fairly constant. This is in contrast to β -cooling where disc is very cold and the spirals set the temperature.*
- *Hence, the morphology of the spiral structures is different. They are weaker, and less numerous. Additionally, the disc becomes more stable over time as the surface density of the disc decreases.*